

Additive fault tolerant control of nonlinear singularly perturbed systems against actuator fault

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This paper presents the design of an additive fault tolerant control for nonlinear time-invariant singularly perturbed systems against actuator faults based on Lyapunov redesign principle. The overall system is reduced into subsystems with fast and slow dynamic behavior using singular perturbation method. The time scale reduction is carried out when the singular perturbation parameter is set to zero, thus avoiding the numerical stiffness due to the interaction of two different dynamics. The fault tolerant controller is computed in two steps. First, a nominal composite controller is designed using the reduced subsystems. Secondly, an additive part is combined with the basic controller to overcome the fault effect. The derived ε -independent controller guarantees asymptotic stability despite the presence of actuator faults. The Lyapunov stability theory is used to prove the stability provided the singular perturbation parameter is sufficiently small. The theoretical results are simulated using a numerical application.

Key words: nonlinear time-invariant singularly perturbed systems, singular perturbation method, additive fault tolerant control, actuator defect, Lyapunov theory

1 Introduction

Singularly perturbed systems belong to a class of systems having a mathematical model which contains a set of differential equations depending on a small positive parameter, called parameter of singular perturbation, multiplying the derivative terms of a part of the equations. They often occur in the physical systems in engineering field, like power systems, dynamic networks, robots, energy and particles transfer mechanism and so on. Such processes involve interconnected slow and fast dynamics which lead commonly to numerical stiffness in the control design methods. To overcome such problems, the methodology of singular perturbation, based on reduction techniques, is frequently used in the literature. The principle is to decompose the overall system into two subsystems with slow and fast dynamics, so that the actual controller, which depends on the parameter of the singular perturbation, is approached by a composite form of the controllers stabilizing the decomposed subsystems [1–4].

Like other systems, the multi time scale systems can be affected by faults that may prevail the controllers, the actuators, or other system components. In this case, an appropriate control strategy, called fault tolerant or reconfigurable control, is required to guarantee nominal performances despite the faults occurrence. Such control schemes are able to recover system and component performances in case of fault happening and to surmount the constraints caused by the typical control scheme.

The aim of this control scheme is to preserve security of machines and system operators [5–9]. For nonlinear systems, meaningful results are presented in the literature. Two different methods are presented. In passive fault tolerant controller design methods, the controller parameters remain unchangeable throughout the faulty and the fault free case. In this situation, techniques like Hamilton-Jacobi inequality approach and robust pole region assignment method are used [10, 11]. The active methods like sliding mode-based control methods and adaptive backstepping compensation control, by contrast, need an on-line fault detection scheme to achieve fault diagnosis step, and then a procedure to ensure the compensation of detected faults [12, 13]. Diverse techniques are proposed in the literature to design fault tolerant controllers for nonlinear systems. Liang and Xu in [14] proposed a variable structure stabilizing control law to tolerate the presence of actuator fault in a nonlinear system. The derived control scheme doesn't require the solution of Hamilton-Jacobi inequality. Benosman and Lum in [15] developed a Lyapunov-based passive feedback controller to guarantee stability of nonlinear affine system with actuator faults. Ma and Yang in [16] designed a fault diagnosis procedure and an active reconfigurable control strategy for nonlinear uncertain dynamic system against time-varying actuator fault. An improved high gain observer is realized to supply more on-line information to generate the reconfigurable controller.

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On the other hand, several approaches to control multi time scale systems have been proposed. Especially, in linear case, Li *et al* in [17] derived a linear quadratic control scheme for singularly perturbed systems. The designed controller is reliable to actuator failures; it is based on fast and slow sub-controllers so that it becomes independent of the singular perturbation parameter. In [18], Tellili *et al* proposed a reconfigurable adaptive method to compensate for any defects that may affect the sensors and the actuators in presence of external perturbation. In both cases, sensor and actuator fault, a controller for the original system was designed and then simplified using singular perturbation method. In nonlinear case, reconfigurable control was investigated by some authors in case of systems undergoing actuator saturation [19–21]. In particular, the methods used to control nonlinear time-invariant singularly perturbed systems did not consider actuator additive faults.

The principal contribution of this work is to develop a control strategy for nonlinear time-invariant singularly perturbed systems affected by actuator additive faults, without going through the linearization of the nonlinear system. The control scheme is a combination of a composite control and an additive part used to accommodate the presence of a fault. The singular perturbation method will be exploited to avoid the numerical stiffness induced by the interconnection of the fast and slow dynamics. Thereby, the reliable controller will be independent of the singular perturbation parameter.

The succeeding paper sections are arranged as follows. In Section 2, the system structure and the problem formulation will be depicted. The main results are formulated in Section 3. An application in form of a simulation is illustrated in Section 4. Finally, a conclusion ends the paper.

2 System characterization and problem formulation

The following nonlinear two-time scales time-invariant singularly perturbed system will be considered [22, 23]

$$\begin{aligned}\dot{x}(t) &= f_1(x, y) + g_1(x, y)u(t) \\ \varepsilon \dot{y}(t) &= f_2(x, y) + g_2(x, y)u(t)\end{aligned}\quad (1)$$

where $x \in B_x \subset \mathbb{R}^{n_1}$ and $y \in B_y \subset \mathbb{R}^{n_2}$ represent the state vectors, $u \in \mathbb{R}^m$ corresponds to the control vector. For $i = 1, 2$, f_i and g_i are locally Lipschitz in a field enclosing the origin and f_i satisfies $f_i(0, 0) = 0$. The scalar ε is a singular perturbation parameter taking values between 0 and 1; it characterizes the time scale separation between the slow and the fast dynamics. $(x, y) = (0, 0)$ is assumed to be an isolated equilibrium state.

The singular perturbation theory will be used to approximate the slow and fast dynamics by setting $\varepsilon = 0$ in the \dot{y} -equation and solving for y in terms of x [1, 24, 25]. It follows for the second equation in system (1)

$$0 = f_2(x, y) + g_2(x, y)u(t). \quad (2)$$

The singularly perturbed system is supposed to be standard, which means, the equation (2) has only a solution $y = h(x, u_s)$, where u_s is the slow part of the control u . Substituting this solution into the first equation of system (1), the following reduced slow subsystem is obtained

$$\dot{x}(t) = f_1(x, h(x, u_s)) + g_1(x, h(x, u_s))u_s(t). \quad (3)$$

It is assumed that only the origin of the closed-loop slow subsystem (3) is an asymptotically stable equilibrium, so there exists a feedback slow control law $u_s(t) = p_s(x)$, where p_s is locally Lipschitz vector function, that renders the slow dynamics asymptotically stable; we consider also a positive definite Lyapunov function $V_s(x)$ guaranteeing for all $x \in B_x$,

$$\frac{\partial V_s(x)}{\partial x} [f_1(x, h(x, u_s)) + g_1(x, h(x, u_s))u_s] \leq -aL_s^2(x) \quad (4)$$

Where $a \succ 0$ and $L_s(x)$ is a positive definite function. The reduced fast subsystem is generated by

$$\frac{dy}{d\tau} = f_2(x, y) + g_2(x, y)(u_s + u_f) \quad (5)$$

in which the fast time scale is defined as $\tau = t/\varepsilon$ and x is assumed to be a constant parameter equal to its initial value. There exists a feedback fast control law $u_f(t) = p_f(x, y)$ which asymptotically stabilizes the fast dynamics, such that the equilibrium $y = h(x, u_s)$ of the closed loop fast subsystem is supposed asymptotically stable uniformly in $x \in \mathbb{R}^{n_1}$. The fast controller satisfies $p_f(x, h(x, p_s(x))) = 0$, where p_f is locally Lipschitz vector function. The composite control of the global system is expressed as a sum of the fast and slow sub-controllers [1, 25, 26]

$$u = u_s(x) + u_f(x, y). \quad (6)$$

The composite feed-back control is designed so that the origin is an asymptotically stable equilibrium of the singularly perturbed closed-loop system (1). For the fast subsystem (5), $V_f(x, y)$ is defined as a positive definite Lyapunov function such that for all $(x, y) \in B_x \times B_y$

$$\begin{aligned}\frac{\partial V_f}{\partial y} [f_2(x, y) + g_2(x, y)(p_s + p_f)] \leq \\ -bL_f^2(y - h(x, p_s))\end{aligned}\quad (7)$$

where $b \succ 0$ and L_f is a positive definite function.

A composite Lyapunov function candidate for the singularly perturbed system (1) is defined by a weighted sum

of the Lyapunov functions for the reduced fast and slow subsystems, so that

$$W(x, y) = (1 - d)V_s + dV_f \quad (8)$$

where $0 < d < 1$ is a free parameter to be chosen.

The composite Lyapunov function $w(x, y)$ will be derived along the trajectories of (1):

$$\begin{aligned} \frac{\partial W(x, y)}{\partial t} = & (1 - d) \frac{\partial V_s(x)}{\partial x} \frac{\partial x}{\partial t} \\ & + d \left(\frac{\partial V_f(x, y)}{\partial x} \frac{\partial x}{\partial t} + \frac{\partial V_f(x, y)}{\partial y} \frac{\partial y}{\partial t} \right). \end{aligned} \quad (9)$$

Using equation (1), we get

$$\begin{aligned} \frac{\partial W(x, y)}{\partial t} = & (1 - d) \frac{\partial V_s(x)}{\partial x} [f_1(x, y) + g_1(x, y)u] \\ & + \frac{d}{\varepsilon} \frac{\partial V_f(x, y)}{\partial y} [f_2(x, y) + g_2(x, y)u] \\ & + d \frac{\partial V_f(x, y)}{\partial x} [f_1(x, y) + g_1(x, y)u]. \end{aligned} \quad (10)$$

After some algebraic manipulations, (10) can be expressed as

$$\begin{aligned} \frac{\partial W(x, y)}{\partial t} = & \frac{d}{\varepsilon} \frac{\partial V_f(x, y)}{\partial y} [f_2(x, y) + g_2(x, y)u] \\ & + (1 - d) \frac{\partial V_s(x)}{\partial x} [f_1(x, h(x, u_s)) \\ & + g_1(x, h(x, u_s))u_s] + T(x, y, u, u_s) \end{aligned} \quad (11)$$

where

$$\begin{aligned} T(x, y, u, u_s) = & (1 - d) \frac{\partial V_s(x)}{\partial x} [f_1(x, y) + g_1(x, y)u \\ & - f_1(x, h(x, u_s)) - g_1(x, h(x, u_s))u_s] \\ & + d \frac{\partial V_f(x, y)}{\partial x} [f_1(x, y) + g_1(x, y)u]. \end{aligned}$$

The first and the second term of the equation (11) represent the derivatives of V_f and V_s along the trajectories of the fast and slow subsystems respectively. From equations (4) and (7), we can see that these two terms are negative definite in x and y . The last term $T(x, y, u, u_s)$ represents the impact of the interconnection among the fast and slow dynamics. This term can be neglected if singular perturbation parameter ε remains small [27].

Using inequalities (4) and (7), equation (11) can be rearranged further to get

$$\frac{\partial W(x, y)}{\partial t} \leq -N(x, y) \quad (12)$$

where $N(x, y) = aL_s^2(x) + \frac{d}{\varepsilon} bL_f^2(y - h(x, p_s))$ is positive definite. Consequently, the composite control (6) ensures that the closed-loop system (1) admits an asymptotically stable equilibrium at the origin for a given interval of the parameter ε and $w(x, y)$ is a Lyapunov function of this system [1, 24, 28].

3 Principal results

In the following, the essential results will be presented. Suppose that the reduced fast and slow subsystems are stabilizable in the domain $B_x \times B_y$ and the state (x, y) is accessible for feedback, we seek for a control scheme in order to stabilize asymptotically the point $(x = 0, y = 0)$ of the closed-loop overall two time scales singularly perturbed system despite actuator fault occurrence.

The system (1), where the actuator is affected with additive fault, can be expressed as

$$\begin{aligned} \dot{x}(t) &= f_1(x, y) + g_1(x, y)(u + D(t, x, y)), \\ \varepsilon \dot{y}(t) &= f_2(x, y) + g_2(x, y)(u + D(t, x, y)) \end{aligned} \quad (13)$$

where $D(t, x, y)$ represents an actuator fault which verifies $\|D(t, x, y)\| \leq B(t, x, y)$ and $B(t, x, y)$ is a non-negative continuous function. The controller takes the form

$$u = u_{\text{nom}} + u_{\text{add}} \quad (14)$$

where $u = u_{\text{nom}}$ represents the nominal controller that stabilizes the overall system in case of a faultless actuator, it corresponds to the composite controller (6). u_{add} denotes the additive part to be designed in order to remove the fault effect in the actuator. The proposed fault tolerant controller to stabilize the faulty system (13) is

$$u = u_{\text{nom}} + u_{\text{add}} \quad (15)$$

where

$$u_{\text{add}} = -B \frac{(1 - d) \frac{\partial V_s(x)}{\partial x} g_1 + d \frac{\partial V_f(x, y)}{\partial y} g_2}{\left\| (1 - d) \frac{\partial V_s(x)}{\partial x} g_1 + d \frac{\partial V_f(x, y)}{\partial y} g_2 \right\|},$$

$(\cdot)^\top$ denotes the transpose of (\cdot) and $\|(\cdot)\|$ the Euclidian norm of (\cdot) .

The next theorem is presented to accomplish the control of the nonlinear singularly perturbed system (13) even when some actuators operate abnormally.

THEOREM 1. *The faulty nonlinear singularly perturbed system given by (13) is considered. Suppose that the reduced fast and slow subsystems are stabilizable and the actuator fault is bounded. Then there exists a singular perturbation parameter $\varepsilon^* > 0$ such that for all $\varepsilon \in (0, \varepsilon^*]$, the origin $(x, y) = (0, 0)$ of the faulty nonlinear singularly perturbed system is locally asymptotically stable under the fault tolerant control law (15) even when the actuators undergo abnormal operation.*

P r o o f . According to equations (13) and (14), it follows for the closed-loop faulty nonlinear singularly perturbed system

$$\begin{aligned} \dot{x}(t) &= f_1(x, y) + g_1(x, y)(u_{\text{nom}} + u_{\text{add}} + D(t, x, y)), \\ \varepsilon \dot{y}(t) &= f_2(x, y) + g_2(x, y)(u_{\text{nom}} + u_{\text{add}} + D(t, x, y)). \end{aligned} \quad (16)$$

An ε -dependent Lyapunov function candidate will be designed,

$$W(\varepsilon, x, y) = (1 - d)V_s + \varepsilon dV_f. \quad (17)$$

The derivative of $W(\varepsilon, x, y)$ will be established along the trajectories of system (16), this leads to

$$\begin{aligned} \frac{\partial W(\varepsilon, x, y)}{\partial t} &= d \frac{\partial V_f(x, y)}{\partial y} [f_2 + g_2(u_{\text{nom}} + u_{\text{add}} + D)] \\ &+ (1 - d) \frac{\partial V_s(x)}{\partial x} [f_1 + g_1(u_{\text{nom}} + u_{\text{add}} + D)] \\ &+ d\varepsilon \frac{\partial V_f(x, y)}{\partial x} [f_1 + g_1(u_{\text{nom}} + u_{\text{add}} + D)]. \end{aligned} \quad (18)$$

The isolation of the terms depending on the nominal control yields the following system

$$\begin{aligned} \frac{\partial W(\varepsilon, x, y)}{\partial t} &= d \frac{\partial V_f(x, y)}{\partial y} (f_2 + g_2 u_{\text{nom}}) \\ &+ (1 - d) \frac{\partial V_s(x)}{\partial x} (f_1 + g_1 u_{\text{nom}}) + d\varepsilon \frac{\partial V_f(x, y)}{\partial x} (f_1 + g_1 u_{\text{nom}}) \\ &+ (1 - d) \frac{\partial V_s(x)}{\partial x} g_1 (u_{\text{add}} + D) + d \frac{\partial V_f(x, y)}{\partial y} g_2 (u_{\text{add}} + D) \\ &+ d\varepsilon \frac{\partial V_f(x, y)}{\partial x} g_1 (u_{\text{add}} + D). \end{aligned} \quad (19)$$

Set $R_1^\top = \frac{\partial V_s(x)}{\partial x} g_1$, $R_2^\top = \frac{\partial V_f(x, y)}{\partial y} g_2$, $R_3^\top = \frac{\partial V_f(x, y)}{\partial x} g_1$ and taking into account inequality (12), the equation takes the form

$$\begin{aligned} \frac{\partial W(\varepsilon, x, y)}{\partial t} &\leq -N(x, y) + (1 - d)R_1^\top (u_{\text{add}} + D) \\ &+ dR_2^\top (u_{\text{add}} + D) + d\varepsilon R_3^\top (u_{\text{add}} + D) \end{aligned} \quad (20)$$

which can be rearranged in the following inequality

$$\begin{aligned} \frac{\partial W(\varepsilon, x, y)}{\partial t} &\leq -N(x, y) + ((1 - d)R_1^\top + dR_2^\top) u_{\text{add}} \\ &+ d\varepsilon R_3^\top u_{\text{add}} + ((1 - d)R_1^\top + dR_2^\top + d\varepsilon R_3^\top) D. \end{aligned} \quad (21)$$

The term $N(x, y)$ is defined as in (12). Using the singular perturbation procedure by setting the singular perturbation parameter ε to zero and considering the upper bound of the fault leads to the following expression

$$\begin{aligned} \frac{\partial W(0, x, y)}{\partial t} &\leq -N(x, y) + ((1 - d)R_1^\top + dR_2^\top) u_{\text{add}} \\ &+ \|((1 - d)R_1^\top + dR_2^\top)\| B \end{aligned} \quad (22)$$

The term $N(x, y)$ is due to the nominal composite control of the fault-free overall system, this term is positive definite in x and y by (12). Whereas the second and third terms designate, respectively, the effect of the additive control u_{add} and the fault $D(t, x, y)$ on $\dot{W}(x, y)$. Consequently, u_{add} will be chosen to remove the influence of the actuator fault $D(t, x, y)$ on $\dot{W}(x, y)$ so that the right term of inequality (22) remains negative definite.

In view of the control law (15) and taking into account the assumptions about the fault, it is obvious that $\dot{W}(x, y) \leq 0$. Thus, it can be concluded that the origin $(x, y) = (0, 0)$ of the faulty overall system is a locally asymptotically stable equilibrium point for the system (16) under the fault tolerant control law (15) for any singular perturbation parameter $\varepsilon \in (0, \varepsilon^*)$.

Remark . The discontinuity of the control law (15) may engender chattering effect. This problem is commonly overcome by approximating the discontinuous function by a saturation function.

4 Example of application

To depict the efficiency of the studied reconfigurable control scheme, the following nonlinear singularly perturbed system is considered

$$\begin{aligned} \dot{x} &= y - x, \\ \varepsilon \dot{y} &= -x - e^y + 1 + u. \end{aligned} \quad (23)$$

The reduced slow subsystem is established by letting $\varepsilon = 0$ in (23). It takes the form

$$\dot{x} = \log_e(-x + 1 + u_s) - x \quad (24)$$

and the slow part of the state y is expressed as

$$y_s = \log_e(-x + 1 + u_s). \quad (25)$$

It is easy to deduce that the control of the slow subsystem $u_s = x - 1 + e^{-x}$ ensures that the closed-loop reduced slow subsystem (24) becomes asymptotically stabilizing about the origin. A corresponding slow Lyapunov function candidate is $V_s = 0.5x^2$. The reduced fast subsystem is given by

$$\frac{dy}{d\tau} = -x - e^y + 1 + u_s + u_f. \quad (26)$$

Taking into account the above mentioned slow control, the fast control $u_f = e^y - e^{-x} - y_f$ stabilizes the state y about the origin. y_f is the fast part of the state y , such that $y_f = y - y_s$. A corresponding fast Lyapunov function candidate is $V_f = 0.5y_f^2 = 0.5(x + y)^2$. The composite control, considered as the nominal control of the fault free overall system, will be designed as the sum of the slow and fast sub-controllers, taking the following form

$$u_{\text{comp}} = u_s + u_f = e^y - y - 1. \quad (27)$$

The resulting closed-loop overall system, after substituting of (27) in (23) is

$$\begin{aligned} \dot{x} &= -x + y, \\ \varepsilon \dot{y} &= -x - y \end{aligned} \quad (28)$$

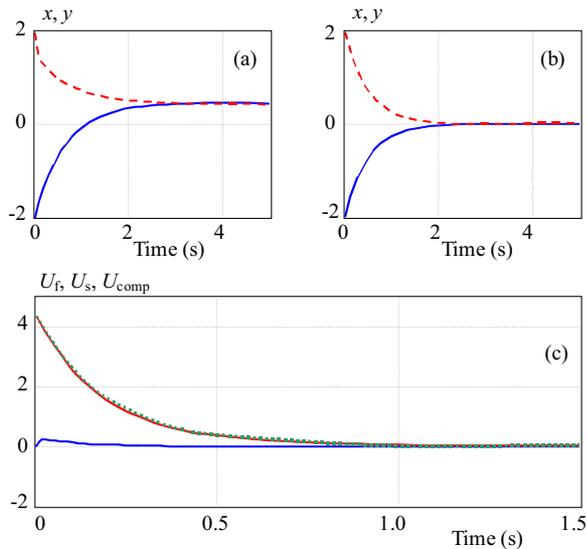


Fig. 1. States trajectories in fault-free case. (a) — x (dashed line) and y (solid line) in open-loop, (b) — States in closed-loop with composite control, (c) — fast (-), slow (-) and composite (-) controllers by $\varepsilon = 0.01$

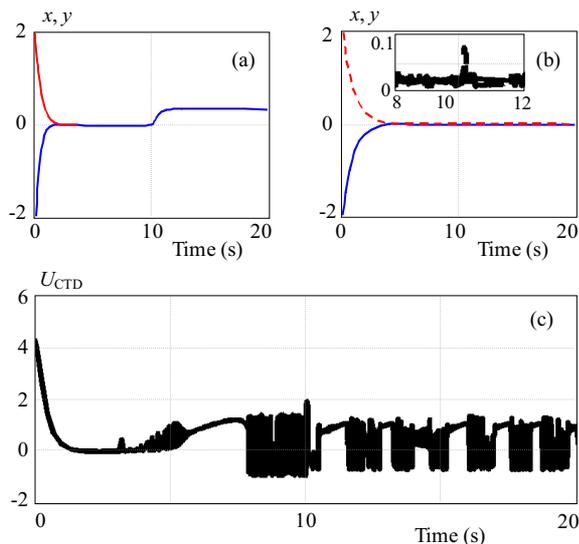


Fig. 2. States trajectories after the appearance of the actuator fault. (a) — x (dashed line) and y (solid line) in case of nominal control, (b) — states in case of fault tolerant control, (c) — fault tolerant control controller by $\varepsilon = 0.01$

where the real parts of the eigenvalues remain negative. This concludes that the origin of system (28) gets an asymptotically stable equilibrium of the closed-loop system. The simulation results in Fig. 1 show the composite control and the states trajectories in the fault-free case, starting from $(x_0, y_0) = (-2, 2)$. It is clear that the composite control (27) ensures the asymptotical stability of the origin.

However, the occurrence of constant additive actuator fault of amplitude 0.7, at time instance 10 sec, yields a loss of the actuator performance. Consequently, the states drive to another stationary point (see Fig. 2(a)). This means that the composite controller is not able to stabilize the origin equilibrium point in the faulty case.

Next, a fault tolerant control scheme will be proposed, according to the equation (15), to compensate for the actuator fault, it takes the form

$$u = u_{\text{comp}} + u_{\text{add}} = e^y - y - 1 - 0.7 \frac{x + y}{\|x + y\|}. \quad (29)$$

Figure 2(b) depicts that the states deviation is corrected using the fault tolerant control (28) and the singularly perturbed system stabilizes at the origin equilibrium point, despite the presence of actuator faults. The zoom in Fig. 2(b) illustrates the effect of fault on the states when the fault tolerant control is used. Figure 2(c) shows the corresponding fault tolerant control which presents high chattering effect.

To solve this problem, the discontinuous function will be changed with a saturation function. The simulation results in Fig. 3(a) and (b) represent, respectively, the states and the controller after the substitution of the discontinuity in the control law. It is clear that the chattering effect is reduced and the states remain at the same equilibrium point.

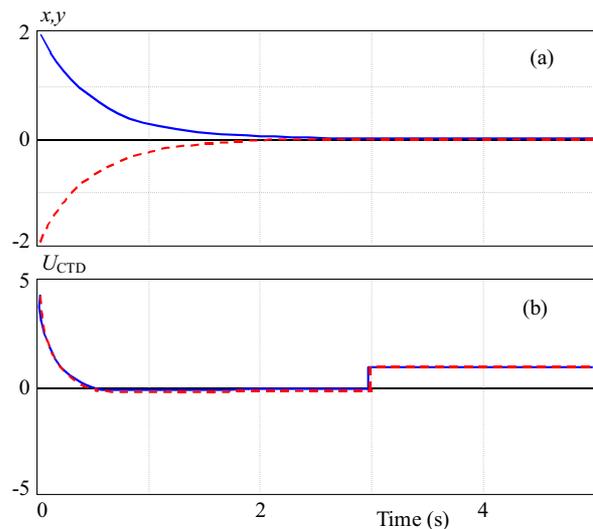


Fig. 3. States trajectories (a) — and fault tolerant control (b) — after the attenuation of chattering effect

5 Conclusion

The control for nonlinear singularly perturbed systems subject to actuator fault is considered. The control scheme involves two parts. First, a composite controller, depending on fast and slow sub-controllers, is designed to treat the nominal case. The second part is generated to deal with actuator faults in additive form. The Lyapunov function for the overall system is designed in composite weighted form using the slow and fast local Lyapunov functions. To ensure the stability in presence of additive

fault, which means that the time derivative of the Lyapunov functions is negative definite, an additive controller will be designed using slow and fast subsystems. A further extension to this work can be the examination of other forms of faults like loss of effectiveness in presence of external perturbation and the consideration of non standard singularly perturbed systems.

In the illustrative example, it is shown that the composite control was unable to hold the origin as an asymptotically stable equilibrium of the overall system, whereas, the use of the reconfigurable control eliminates the effect of actuator failure from the states trajectories.

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