COMBINED OPERATION OF AC AND DC DISTRIBUTION SYSTEM WITH DISTRIBUTED GENERATION UNITS

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This paper presents a DC distribution system which has been supplied by external AC systems as well as local DG units in order to demonstrate an overall solution to power quality issues. In this paper, the proposed operation method is demonstrated by simulation of power transfer between external AC systems, DG units, AC and DC loads. The power flow control in DC distribution system has been achieved by network converters and DG converters. Also, the mathematical model of the network, DG and load converters are obtained by using the average technique, which allows converter systems accurately simulated and control strategies for this converters is achieved. A suitable control strategy for network converters has been proposed that involves DC voltage droop regulator and novel instantaneous power regulation scheme. Also, a novel control technique has been proposed for DG converters. In this paper, a novel control system based on stationary and synchronously rotating reference frame has been proposed for load converters for supplying AC loads connected to the DC bus by balanced voltages. The several case studies have been studied based on proposed methods. The simulation results show that DC distribution systems including DG units can improve the power quality at the point of common coupling (PCC) in the power distribution system or industrial power system.

Key words: power quality, DC distribution system, distributed generation, microturbine unit, fuel cell unit

1 INTRODUCTION

Custom power devices have widely studied by many researchers as an ultimate method to improve power quality [1, 2]. The function of custom power devices is to mitigate the disturbances that affect the performance of the critical loads. Series custom power device injects an active power (P) and reactive power (Q) into the distribution system to achieve voltage compensation [3, 4]. Also, parallel custom power device injects P and Q to achieve current compensation [5, 6]. Combined series and parallel custom power devices inject P and Q to achieve both voltage and current compensations [7, 8]. Most of these devices can not compensate the voltage interruptions because they have no energy storage in their DC link. These devices have been used to solve specific power quality problems such as voltage sags, swells, outages, flickers, and harmonics. However, co-ordination of these custom power devices for power quality and reliability enhancement is quite a hard task. The interest in DG has been rapidly increasing because DG is considered to play an important role in the future power system [9, 10]. Several studies have proposed the interconnection of DG units with power systems using voltage-source-converters (VSCs) as versatility of VSCs helps in improving the ability of DG [11–13], [25, 26]. Moreover, the power electronic interface for DG units has the ability to control the voltage and current disturbances. As a result, the integration of DG units in AC and DC distribution systems provides additional performance which is superior to the combination of the UPS system and custom power devices. It is shown that DC distribution systems offer high power density, high efficiency and tightly regulated output voltage as needed by telecommunication equipments, shipboard systems and traction systems [14–17]. This paper proposes a combined AC and DC distribution system including DG units. The advantage of the proposed system over the custom power devices is that it can compensate voltage interruptions, as well as voltage sags, voltage swells, harmonics, and the reactive power. The simulation results show that the proposed system can improve the power quality at the point of installation in the distribution system or industrial power system.

2 DC DISTRIBUTION SYSTEM CONFIGURATION

Figure 1 shows the DC distribution system considered for study in this paper. The proposed system is equipped with generating sources in the form of DGs, instead of UPSs. The DC bus is assumed to be lossless and is connected to the AC distribution system by two AC-to-DC network converters in order to enhance the system reliability. These converters are assumed to have equal power ratings [1]. Considering the merits of VSCs [1], [18], they are employed as interface between AC grid and DC bus. The power fed to the DC bus is supplied by two external AC feeders. These feeders are assumed to be connected to independent substations. In this system, it is assumed that two fuel cell units, with equal power ratings, are connected to the DC bus via DC-to-DC converters while two microturbine units, with equal power...
ratings, are connected to the DC bus through diode rectifier and DC-to-DC converter. The DC-to-DC converters are called as DG converters. The chosen number of each DG units is arbitrary. The loads fed by DC bus, in Fig. 1, can be divided into four categories

- a) L1 is a sensitive or critical load, which requires uninterrupted sinusoidal voltage.
- b) L2 is a nonlinear load, which draws harmonic currents.
- c) L3 is an unbalanced AC load which draws unbalanced currents.
- d) L4 is a DC load directly connected to the DC bus.

Power balancing in DC bus could be achieved by AC-to-DC network converters equipped with DC voltage regulator, which adjust the DC voltage at acceptable limit during steady state and dynamic conditions. Therefore, the active power of DG units can be injected to the DC bus and all the loads connected to the DC bus can be supplied with the constant DC voltage. The power regulation of DGs can be specified by various criteria such as maximum efficiency conditions or thermal load requirements [19]. Thus, considering both technical and economical constraints, the control system of DGs converters should not be designed to support the power balancing for DC bus. In the system, shown in Fig. 1, the energy storage system is not required to support the DC voltage. The objective of this system selection is to demonstrate the overall solution to power quality, reliability, energy-delivery efficiency problems due to lack of energy storage system and the possibility of the DC bus utilization in parallel with external AC network or in islanding mode during AC grid outages.

3 POWER MANAGEMENT STRATEGY

The objective of the power management strategy is to achieve optimal operational performance providing high power quality, reliability and efficient energy dispatch. Power management strategy of network converters should
provide the reference active and reactive power signals for the power regulation. The reference active power signal of a network converter is determined by the DC voltage regulator system, which will be discussed in the next section. The reference reactive power of a network converter in AC side is specified by its reactive power management strategy which is usually Unity Power Factor (UPF) operation mode [20, 21]. The reference active power of a DG unit is specified by its power management system. The generators supplied by non-renewable sources, such as microturbines and fuel cells, the active power management strategies consider various criteria, such as maximum efficiency conditions or thermal load requirements [19]. In synchronous generators connected to microturbine, power factor control, eg UPF, is usually adopted to maximize the active power generation [20-22]. For the system, shown in Fig. 1, the following assumptions have been made:

a) The proposed control strategy is based on locally measured signals since no communication exists among DG units and network converters.

b) The control scheme of the network converter is based on the control loop feedback of the DC voltage because this is the only common signal for power balancing in DC bus. Moreover, each network converter is equipped with DC voltage regulator with relatively slow response for real power control.

c) Each network converter should inject the power from the external AC network to the DC bus if the available DC power generation is not sufficient for supplying the system loads.

d) None of the DG units acts as a spinning reserve or as a back-up generator.

e) DG units are expected to supply pre-specified power, e.g. to minimize power import from the grid (peak shaving strategy).

f) Simple, fast and flexible real/reactive power control strategies are required to damp the proposed system oscillations, eg, due to islanding. (This cant be the assumption)

The dynamic model for the DC side of the system is shown in Fig. 2. Two network converters, connected in parallel, can be modeled by current sources controlled by DC bus voltage signal. These converters distribute the current changes between themselves. In addition, the power reference for two bidirectional network converters is provided by DC voltage regulator. The DG unit converters and load converters are operating in the current control mode. The control philosophy for two network converters is based on feedback from the DC bus voltage, $V_{dc}$, and the reference value for the DC bus voltage. If the DC bus voltage is low, the power should be injected to the DC bus by DG units or the external AC systems. If the DC bus voltage is high, the surplus power in DC bus must be returned to external AC systems. As it can be seen in Fig. 2, we have

$$I_{n1}(s) + I_{n2}(s) - (C_s + C_r)sV_{dc}(s) = I_{n1}(s) + I_{n2}(s) - I_{L3}(s) + I_{L4}(s) - I_{MTS}(s) - I_{FCS}(s) = I_{net}(s)$$

where, $I_{n1}$ and $I_{n2}$ are the output currents of network converters No. 1 and No. 2 respectively. $I_{MTS}$ and $I_{FCS}$ are the output currents of microturbine and fuel cell units respectively. $I_{L1}$, $I_{L2}$ and $I_{L3}$ are the output currents of load converters No. 1, No. 2 and No. 3 respectively. $I_{L4}$ is the current drawn by the load directly connected to the DC bus. $I_{net}$ is the current difference between the output current of all loads and DG units connected to the DC bus. $C_s$ is the equivalent capacitance of the network, storage and DG converters. Also $C_r$ is the equivalent capacitance of the load converters. $V_{dc,ref1}$ and $V_{dc,ref2}$ are DC reference voltage and the output current of the $i$-th network converter respectively. $P_{ni}$ and $R_{ni}$ are the output DC power and the equivalent resistance of the $i$-th network converter respectively. The measured DC bus voltage is low pass filtered to attenuate the interaction between the negative sequence voltage of the AC side and DC bus voltage control and to enhance controller pole placement. $\omega_p$ is the break-over frequency of the low pass filter (shown with LPF in Fig. 2). Considering equations (1), (2) and (3), the measured voltage, the reference voltages in DC bus ($V_{dc,ref1}$ and $V_{dc,ref2}$) and the current difference between the output current of all loads and DG units ($I_{net}$) can be presented in one block diagram as shown in Fig. 3(a). This figure shows the main structure of the DC bus voltage droop controller for the network converters. $C_{dc}$ which is equal to $C_s + C_r$, is the total equivalent capacitance of converters connected to the DC bus. From Fig. 3(a), we have

$$V_{dc}(s) = \frac{1}{R_{dcC_{dc}}} \left( s + \omega_p \right) \left( s + \omega_p \right) V_{dc,ref1}(s) + \frac{R_{n1} + R_{n2}}{R_{n1}R_{n2}C_{dc}} \frac{\omega_p}{R_{dcC_{dc}}} V_{dc,ref2}(s) - \frac{1}{R_{dcC_{dc}}} \left( s + \omega_p \right) I_{net}(s).$$

The closed loop transfer function is given by the following equation

$$P(s) = s^2 + \omega_p s + \frac{R_{n1} + R_{n2}}{R_{n1}R_{n2}C_{dc}}\omega_p.$$

The desired characteristic equation can be expressed as

$$P(s) = s^2 + 2\zeta_n \omega_n s + \omega_n^2$$

where, $\zeta_n$ and $\omega_n$ are the desired closed loop damping and bandwidth, respectively. The value of DC bus equivalent capacitors determines the performance of the DC
For \( P_{ni} \) we have

\[
P_{ni} = V_{dc}I_{ni} = \frac{V_{dc}(V_{dc,refn1} - V_{dc})}{R_{ni}}, \quad i = 1, 2.
\]  

(10)

Substituting equation (9) in the equation (8) we get

\[
V_{dc} = \frac{R_{n2}V_{dc,refn1} + R_{n1}V_{dc,refn2} - R_{n1}R_{n2}I_{net}}{R_{n1} + R_{n2}}.
\]  

(11)

Using equations (9) and (11), we obtain

\[
I_{n1} = \frac{R_{n2}I_{net}}{R_{n1} + R_{n2}} + \frac{V_{dc,refn1} - V_{dc,refn2}}{R_{n1} + R_{n2}},
\]  

(12)

\[
I_{n2} = \frac{R_{n1}I_{net}}{R_{n1} + R_{n2}} - \frac{V_{dc,refn1} - V_{dc,refn2}}{R_{n1} + R_{n2}}.
\]  

(13)

\[
I_c = \frac{V_{dc,refn1} - V_{dc,refn2}}{R_{n1} + R_{n2}}.
\]  

(14)

It is clear that if \( V_{dc,refn1} = V_{dc,refn2} = V_{dc,ref} \), then the circulating current, \( I_c \), is equal to zero. In addition, if \( R_{n1} = R_{n2} = R_n \), then the injected currents to the DC bus via network converters, \( I_{n1} \) and \( I_{n2} \), are equal. However, the proper load sharing can be obtained by the appropriate selection of \( R_{ni} \). The voltage droop, \( \delta \), can be defined as follows

\[
\delta = \frac{V_{dc,refn1} - V_{dc}}{V_{dc,refn1}} = \frac{V_{dc,refn2} - V_{dc}}{V_{dc,refn2}}.
\]  

(15)

The equation (10) can be rewritten in the following form

\[
P_{ni} = \frac{\delta(1 - \delta)V_{dc,refn1}^2}{R_{ni}}, \quad i = 1, 2.
\]  

(16)

At rated power conditions, equation (16) can be rewritten as follows

\[
P_{ni,rated} = \frac{\delta_n(1 - \delta_n)V_{dc,refn1}^2}{R_{ni,rated}}, \quad i = 1, 2,
\]  

(17)

\[
R_{ni} = \frac{\delta_n(1 - \delta_n)V_{dc,refn1}^2}{P_{ni,rated}}, \quad i = 1, 2.
\]  

(18)
bus voltage exceeds the threshold value. Moreover, if the DC bus capacitor can be determined by the following equation.

\[
C_{dc} = \frac{2C^2_1}{\omega} \left( P_{n1,\text{rated}} + P_{n2,\text{rated}} \right) V_{dc,\text{ref}1} V_{dc,\text{ref}2}.
\]

Equation (19) shows that if \( V_{dc,\text{ref}1} = V_{dc,\text{ref}2} = V_{dc,\text{ref}} \) and \( P_{n1,\text{rated}} = P_{n2,\text{rated}} = P_{n,\text{rated}} \), then the total required DC bus capacitor can be determined by the following equation.

\[
C_{dc} = \frac{4C^2_1 P_{n,\text{rated}}}{\omega \delta_1 V^2_{dc,\text{ref}}}.
\]

Figure 3(b) shows the steady state droop characteristics of network converters. The output current of these converters can be controlled by the slope of the voltage droop characteristics.

For suitable operation of network converters, DC bus voltage can be changed within two threshold values, \( V_{\text{ref}1} \) and \( V_{\text{ref}2} \). By the proposed control strategy for network converters, the DC bus voltage must be kept stable within an acceptable limit. Moreover, if the DC bus voltage exceeds the threshold value \( V_{\text{ref}3} \), the power produced by DG units is cancelled out. In the system, the power difference between the load demands and power generation of DG units is calculated as follows.

\[
P_{\text{net}} = P_{L1} + P_{L2} + P_{L3} + P_{L4} - \sum_{n=1}^{2} P_{FC,n} - \sum_{n=1}^{2} P_{MT,n}.
\]

Equation (21) shows that if \( P_{n1} + P_{n2} = P_{\text{net}} \), then the power generation by network converters to the DC bus, \( P_{n1} \) and \( P_{n2} \), can be in the following modes.

a) If \( P_{\text{net}} < 0 \), then the power generation by DG units has been increased or the power consumed by loads has been reduced. In this case, the additional power available in the DC bus could be injected to the AC grid via network converter.

b) If \( P_{\text{net}} > 0 \), then the power generation by DG units has been reduced or the power consumed by loads has been increased. In this case the AC power has been injected to the network converter by the AC grid, in order to supply the DC bus.

c) If \( P_{\text{net}} = 0 \), then the power generation from DG units is absorbed by the all loads connected to the DC bus. In this case, the AC power injected to the DC bus via network converters is zero.

4 CONTROL STRATEGIES OF CONVERTERS

The objective of the converters, connected to the DC bus is to enhance the power quality, reliability and energy efficiency of the system. In this paper, suitable control strategies for each converter are presented. These strategies are mainly based on the control of the DC bus voltage within acceptable limit.

4.1 Circuit configuration and control scheme of network converters

The equivalent circuit of network converter is shown in Fig. 4. The converter is represented with three ideal current sources \( i_{ref}^{c}, i_{ref}^{b} \) and \( i_{ref}^{f} \). The converter manages the amount of current injected to the DC bus and vice versa. As it can be seen in Fig. 4, the input signals of network converter controller are the source phase voltages, \( v_{sa}, v_{sb} \) and \( v_{sc} \), the source line currents, \( i_{sa}, i_{sb} \) and \( i_{sc} \), the three phase output currents for this converter \( i_{fa}, i_{fb}, i_{fc} \), DC bus voltage \( V_{dc} \) and reference DC voltage \( V_{dc,\text{ref}} \). \( L_f \) is the inductance of the converter filter. \( R_s \) and \( L_s \) are the resistance and inductance of the AC grid. This controller uses the hysteresis current control (HCC) switching technique to reduce the high switching
The circuit configuration and control scheme for each converter has been depicted in Fig. 5. The main part of this scheme is DC voltage regulator. In this paper, the droop control strategy has been used for the network converter, since it does not require any communication system. More details of the DC voltage regulator are shown in Fig. 6. It is obvious that the DC voltage error can be fed to the droop controller, whose droop is \( K_n \), in order to obtain the injected current (ie, \( i_n \)) to the DC bus. The multiplication of \( v_{dc} \) and \( i_n \) determines the injected power to the DC bus of network converter (ie, \( P_n \)). If the DC bus voltage remains between references value, \( V_{ref nl} \) and \( V_{ref nu} \), the signal \( P_n \) is equal to zero, and the network converter does not exchange power with the external AC system. Also, the power required from the loads is entirely supplied by DG units. If the voltage exceeds the higher reference value, \( V_{ref nu} \), the signal \( P_n \) is negative and the network converter supplies power to the external AC system and if it is below the lower reference value, \( V_{ref nl} \), the signal \( P_n \) is positive and it absorbs power from the external AC system. For the regulator shown in Fig. 6, we have

\[
I_n = K_n(V_{dc,ref n} - v_{dc,lp}), \quad (24)
\]

\[
P_n = v_{dc} i_n. \quad (25)
\]

Using equations (24) and (25), we obtain

\[
P_n = K_n v_{dc}(V_{dc,ref n} - v_{dc,lp}). \quad (26)
\]

Equations (24), (25) and (26) in steady state condition can be rewritten as follows

\[
I_n = K_n(V_{dc,ref n} - V_{dc}), \quad (27)
\]

\[
P_n = I_n V_{dc} = K_n v_{dc}(V_{dc,ref n} - V_{dc}). \quad (28)
\]

Considering the equations (12) and (29), the steady state droop is equal to

\[
R_n = \frac{1}{K_n}. \quad (30)
\]

From \( \alpha-\beta-0 \) transformation and the power calculation box in Fig. 5, we get

\[
\begin{bmatrix}
v_{s0} \\
v_{sa} \\
v_{sc}
\end{bmatrix} = T_{\alpha\beta0} \begin{bmatrix}
v_{s0} \\
v_{sa} \\
v_{sc}
\end{bmatrix}, \quad T_{\alpha\beta0} = \begin{bmatrix}
\sqrt{2}/2 & \sqrt{2}/2 & 1/2 \\
-1/2 & -1/2 & -1/2 \\
0 & \sqrt{3}/2 & -\sqrt{3}/2
\end{bmatrix}, \quad (31)
\]

\[
\begin{bmatrix}
i_{s0} \\
i_{sa} \\
i_{sc}
\end{bmatrix} = T_{\alpha\beta0} \begin{bmatrix}
i_{s0} \\
i_{sa} \\
i_{sc}
\end{bmatrix}, \quad (32)
\]

\[
Q_n = -v_{s\beta}i_{s\alpha} + v_{s\alpha}i_{s\beta}. \quad (33)
\]

The reference active power, \( P_n \), can be produced by the DC voltage regulator (equation (26)). In addition, the reference reactive power, \( Q_n \), can be produced by the power calculation box (equation (33)). In this paper, the stationary transformation (Clarke transformation) has been used in order to provide simple and fast control strategy. Thus, the \( \alpha-\beta \) component related to
the reference current of each network converter can be expressed by equation (34).

\[
\begin{bmatrix}
i_{s0ref} \\
i_{sαref} \\
i_{sβref}
\end{bmatrix} = \frac{1}{v_{sα}^2 + v_{sβ}^2} \begin{bmatrix}
v_{sα} & -v_{sβ} \\
v_{sβ} & v_{sα}
\end{bmatrix} \begin{bmatrix}
P_a \\
Q_n
\end{bmatrix} .
\]

(34)

The zero-sequence current in the zero coordinate frame of reference is \(i_{s0}\), and it is clear that

\[i_{s0ref} = i_{s0} .\]

Finally, the \(α−β−0\) inverse transformation box shown in Fig. 5 calculates the three-phase current references to be fed into the hysteresis current control scheme. Thus

\[
\begin{bmatrix}
i_{αref} \\
i_{βref} \\
i_{cref}
\end{bmatrix} = T_{abc} \begin{bmatrix}
i_{s0ref} \\
i_{sαref} \\
i_{sβref}
\end{bmatrix}, \quad T_{abc} = \sqrt{\frac{2}{3}} \begin{bmatrix}
\sqrt{2} & 0 & -1 \\
0 & \sqrt{2} & -\sqrt{2} \\
-1 & -\sqrt{2} & \sqrt{2}
\end{bmatrix} .
\]

(36)

\[
\begin{bmatrix}
i_{αref} \\
i_{βref} \\
i_{cref}
\end{bmatrix} = -\begin{bmatrix}
i_{α} \\
i_{β} \\
i_{c}
\end{bmatrix} .
\]

(37)

The comparison of the calculated reference currents and the actual currents generated by the network converter will result in the error signal, which controls the switches of the converter.

4.2 Circuit configuration and control scheme of distributed generation units

Figure 7(a) shows the dynamic model of each fuel cell unit [24]. Figure 7(b) shows the block diagram of each microturbine (MT) generation unit. MT generation unit has a common rotating shaft, associated with the Permanent Magnet Synchronous Generator (PMSG), compressor, and turbine. PMSG is also connected to the DC bus via three phase unidirectional rectifier as well as DC-to-DC converter [27].

As shown in Fig. 1, DG converters are connected between the DC bus and the DG units. The equivalent circuit of a DG converter is shown in Fig. 8(a). This converter is represented with an ideal current sources, \(i_{fDG}\). The converter manages the amount of current injected to the DC bus. As it can be seen in Fig. 8(a), the input signals of DG converter controller are the DG units output voltage, \(v_{DG} (v_{f_a} \text{ and } v_{f_c})\), the DC bus voltage, \(v_{dc}\), the output current for this converter \(i_{fDG}\) and the reference active power of each DG unit, \(P_{DG,ref}\). It must be noted that the reference active power, \(P_{DG,ref}\), is limited considering the DG energy capacity. The control strategy for each DG converter (ie, DC-to-DC converters in figures 8 and 9) has been shown in Fig. 8(b). In this control scheme, the reference active power, \(P_{DG,ref}\), is specified by the related active power management strategy. The reference current, \(i_{fDG}^\text{ref}\), can be determined as follows

\[
i_{fDG}^\text{ref} = \frac{P_{DG,ref}}{v_{DG}} .
\]

(38)

The comparison of the calculated reference currents \(i_{fDG}^\text{ref}\) and the actual currents generated by the DG converter \(i_{fDG}\) will result in the error signal, which is fed to the HCC system, which determines the switching pattern of DC-to-DC converters.

4.3 Circuit configuration and control scheme of AC loads connected to the DC bus

As shown in Fig. 1, three load converters are connected between the DC bus and the AC loads. The load converter is VSC with neutral clamped DC capacitors. This topology is characterized by the connection of the neutral point of the load to the midpoint of the clamped DC capacitors. The equivalent circuit of load converter is shown in Fig. 9. This converter is represented with three voltage sources, \(v_{f_a}, v_{f_b} \text{ and } v_{f_c}\). The equations describing load converter voltages and currents are expressed by the following equation

\[
\begin{bmatrix}
v_{f_a} \\
v_{f_b} \\
v_{f_c}
\end{bmatrix} = \begin{bmatrix}
v_{la} \\
v_{lb} \\
v_{lc}
\end{bmatrix} + \begin{bmatrix}
L_f & 0 & 0 \\
0 & L_f & 0 \\
0 & 0 & L_f
\end{bmatrix} \frac{d}{dt} \begin{bmatrix}
i_{f_a} \\
i_{f_b} \\
i_{f_c}
\end{bmatrix}
\]

(39)
where, \( v_{fa}, v_{fb} \) and \( v_{fc} \) are the line to neutral three phase output voltages of the load converter. \( i_{fa}, i_{fb} \) and \( i_{fc} \) are three phase output currents. \( v_{la}, v_{lb} \) and \( v_{lc} \) are line to neutral three phase voltages of AC loads.

The voltage equations in the \( d-q-0 \) reference frame are as follows:

\[
\begin{bmatrix}
    v_{fa} \\
    v_{fb} \\
    v_{fc}
\end{bmatrix}
= \begin{bmatrix}
    L_f & 0 & 0 \\
    0 & L_f & 0 \\
    0 & 0 & L_f
\end{bmatrix}
\frac{df}{dt}
\begin{bmatrix}
    i_{fa} \\
    i_{fb} \\
    i_{fc}
\end{bmatrix}
+ \begin{bmatrix}
    0 & -\omega L_f & 0 \\
    \omega L_f & 0 & 0 \\
    0 & 0 & 0
\end{bmatrix}
\begin{bmatrix}
    v_{fa} \\
    v_{fb} \\
    v_{fc}
\end{bmatrix}.
\] (40)

(b) The load phase voltages \( v_{la}, v_{lb} \) and \( v_{lc} \) can be detected and transformed to the stationary reference frame with Clarke transformations and then into \( d-q-0 \) synchronously rotating reference frame using following equations

\[
\begin{bmatrix}
    v_{la} \\
    v_{lb} \\
    v_{lc}
\end{bmatrix}
= T_{\alpha\beta0}
\begin{bmatrix}
    v_{fa} \\
    v_{fb} \\
    v_{fc}
\end{bmatrix},
\] (41)

\[
\begin{bmatrix}
    v_{ld} \\
    v_{lq} \\
    v_{l0}
\end{bmatrix}
= T_{dq0}
\begin{bmatrix}
    v_{la} \\
    v_{lb} \\
    v_{lc}
\end{bmatrix},
\] (42)

\[
T_{dq0} = T_{dq0}^{-1}
\begin{bmatrix}
    \cos(\omega t) & \sin(\omega t) & 0 \\
    \sin(\omega t) & -\cos(\omega t) & 0 \\
    0 & 0 & 1
\end{bmatrix}.
\]

The load phase voltage should be kept balanced and sinusoidal with constant amplitude and frequency. Therefore the expected load voltages in the \( d-q-0 \) reference frame should have only the following values

\[
\begin{bmatrix}
    v_{ld}^{exp} \\
    v_{lq}^{exp} \\
    v_{l0}^{exp}
\end{bmatrix}
= \begin{bmatrix}
    0 \\
    0.4 \sqrt{\frac{2}{3}} \\
    0
\end{bmatrix}.
\] (43)

The reference load current in the \( d-q-0 \) coordinate are:

\[
\begin{bmatrix}
    i_{ld}^{ref} \\
    i_{lq}^{ref} \\
    i_{l0}^{ref}
\end{bmatrix}
= \begin{bmatrix}
    \text{PI}(v_{ld} - v_{ld}^{exp}) \\
    \text{PI}(v_{lq} - v_{lq}^{exp}) \\
    \text{PI}(v_{l0} - v_{l0}^{exp})
\end{bmatrix}.
\] (44)

The output signals from PI controller can be expressed by the equation (45).

\[
\begin{bmatrix}
    i_{ld}^{ref} \\
    i_{lq}^{ref} \\
    i_{l0}^{ref}
\end{bmatrix}
= \begin{bmatrix}
    i_{ld} \\
    i_{lq} \\
    i_{l0}
\end{bmatrix}
+ \begin{bmatrix}
    \text{PI}(i_{ld}^{ref} - i_{ld}) \\
    \text{PI}(i_{lq}^{ref} - i_{lq}) \\
    \text{PI}(i_{l0}^{ref} - i_{l0})
\end{bmatrix}
\begin{bmatrix}
    -\omega L_f i_{fd} \\
    -\omega L_f i_{fq} \\
    0
\end{bmatrix}.
\] (45)

The reference output voltages for the load converter are transformed to the \( a-b-c \) coordinate by using inverse synchronously rotating and stationary reference frames.

\[
\begin{bmatrix}
    v_{afa}^{ref} \\
    v_{fbd}^{ref} \\
    v_{fcf}^{ref}
\end{bmatrix}
= T_{\alpha\beta0}^{-1}
\begin{bmatrix}
    v_{afa}^{ref} \\
    v_{fbd}^{ref} \\
    v_{fcf}^{ref}
\end{bmatrix},
\] (46)

\[
\begin{bmatrix}
    v_{afa}^{ref} \\
    v_{fbd}^{ref} \\
    v_{fcf}^{ref}
\end{bmatrix}
= T_{abc}
\begin{bmatrix}
    v_{afa}^{ref} \\
    v_{fbd}^{ref} \\
    v_{fcf}^{ref}
\end{bmatrix}.
\] (47)

Then the available voltages in the \( a-b-c \) coordinate are compared with the triangular wave provided by PWM voltage control box. Therefore the output provides suitable switching pattern of each DC-to-AC converter.

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![Fig. 11. Phase voltages in AC side of network converter No. 2](image)

![Fig. 12. (up) Active power variations; (down) DC bus voltage](image)
5 SIMULATION RESULTS

The system shown in Fig. 1 has been simulated in PSCAD/EMTDC software. It is assumed that two 50 Kw AC-to-DC network converters are in service. It is also assumed that the reference DC voltage is equal to 750 V and the nominal droop is 5 percent. The rated power for each microturbine and fuel cell unit is assumed to be 20 Kw and 10 Kw respectively. Also, it is assumed that the each microturbine and fuel cell unit is generated the rated power in all of the simulation time. It must be noted that the fuel cell is not able to react fast enough to compensate power fluctuations satisfactorily.

5.1 Voltage interruption in AC distribution system

A three phase fault at bus F2 in Fig. 1 has been modeled to represent a voltage interruption during the time period of \( t = 0 \) s till \( t = 0.5 \) s. Figure 11 illustrates the phase voltages \((V_{a2}, V_{b2} \text{ and } V_{c2})\) at this bus. Figure 12 (up) depicts the variations of the active power in external AC grids \((P_{n1} \text{ and } P_{n2})\), the power of AC and DC loads connected to the DC bus \((\text{ie, } P_{L1} = P_{L1} + P_{L2} + P_{L3} + P_{L4})\) and the output power of DG units injected to the DC bus \((\text{ie } P_{MTs} \text{ and } P_{FCS})\). As it can be seen, the active power of the No. 2 network converter \((P_{n2})\) decreases during the fault (interruption) interval, however the active power of the No. 1 network converter \((P_{n1})\) increases because it acts as a DC voltage regulator. It is clear that during normal operation conditions, two network converters provide the same power to the DC bus while during the voltage interruption; the network converter No. 1 only injects the power to the DC bus. Figure 12 also shows that the injected active powers to the DC bus by DG units is constant. The main reason is that the proposed control strategies for DG converters is able...
to cancel interactions between DG units and neighboring loads.

Figure 12 (down) shows the DC bus voltage which remains constant during voltage interruption using the proposed power regulation scheme for network converters. As it can be seen, the actual DC bus voltage ($V_{dc}$) follows the DC voltage ($V_{dc,dy}$) which is calculated based on the equation (3). Figure 13 shows the line currents of AC loads connected to DC bus. It was found that the load phase currents (L2 and L3) are not sinusoidal. Figure 14 illustrates the phase voltages at the terminal of the sensitive load ($V_{aL1}$, $V_{bL1}$ and $V_{cL1}$), the nonlinear load ($V_{aL2}$, $V_{bL2}$ and $V_{cL2}$) and the unbalanced load ($V_{aL3}$, $V_{bL3}$ and $V_{cL3}$), respectively. It can be seen that high quality voltages have been provided for AC loads. It is clear that the load phase voltage is balanced and sinusoidal with constant amplitude and frequency. To quantify the level of the voltage unbalance, the percentage of unbalance is expressed in accordance with the definition of the “degree of unbalance in three phase system” [28]. In this case, the negative sequence unbalance is lower than 1% which is acceptable with respect to 2% admitted by international standards.

5.2 Reference Power for DG units

In this section, the reference active power of fuel cells has been reduced by 50% of rated power, and subsequently increased to its rated power. Figure 15 (up) shows the instantaneous active power of external AC grids and DG units and AC and DC loads. It can be said that the suggested control strategy for fuel cell converter provides reasonable response. As shown in Fig. 15, the instantaneous active power of network converters ($P_{n1}$ and $P_{n2}$) are equal showing the proper load sharing. Figure 15 (down) also depicts the DC bus voltage with a voltage swell. It is also clear that when the reference of the active power has been increased to the rated power, the DC bus voltage faces to the sag phenomena. As it can be seen,
the actual DC bus voltage \( (V_{dc}) \) follows the DC voltage \( (V_{dc,dy}) \) which is calculated using equation (3).

5.3 Temporary loss of load converter

Figures 16 to 18 show the simulation results due to the loss of load converters No. 2 and No. 3 supplying nonlinear (L2) and unbalanced loads (L3), respectively. Figure 16 shows the line currents of AC loads connected to DC bus due to loss of the associated converters for 0.1 second.

Figure 17 illustrates the phase to ground voltages at the terminal of the sensitive load (\( V_{aL1}, V_{bL1} \) and \( V_{cL1} \)) and the unbalanced load (\( V_{aL3}, V_{bL3} \) and \( V_{cL3} \)), respectively. It can be seen that high quality voltages have been provided for AC loads. It is clear that these voltages are not affected by the loss of the converter. In this case, the negative sequence unbalance is lower then 1% which is acceptable. It should be noticed that international standards admit unbalance lower than 2% [28].

Figure 18 (up) shows the instantaneous active power of external AC grids and DG units as well as AC and DC loads. In this situation due to the loss of the load converter, the network converters return the additional power from the DC bus to the external AC system. Figure 18 (down) shows the DC bus voltage which is within acceptable limit. As it can be seen, the actual DC bus voltage \( (V_{dc}) \) follows the DC voltage \( (V_{dc,dy}) \) which is calculated using equation (3). The other simulation results which are not presented in this paper have been verified by equations (10) and (22).

6 CONCLUSION

This paper proposes a combined operation of the AC and DC distribution system with the DG units. The proposed system can compensate voltage sags and swells as well as voltage interruptions under different operating conditions. The PSCAD/EMTDC software has been used for the modeling and the simulation of the system. We made the main concept of the power management strategy, and then, on the power flow and voltage control. The simulation results show that the proposed strategies provide the suitable load sharing between network converters, while the DC bus voltage remains under acceptable level. The results also show that the proposed system can protect the sensitive loads against disturbances. It is shown that the nonlinear load does not inject harmonic currents to the AC grid and unbalancing would not be occurred in the AC grid. The results also show that the proposed system can supply the unbalanced AC load with balanced voltages. It is shown that the unbalancing would not be occurred in the AC and DC network by the unbalanced AC load.

LIST OF ABBREVIATIONS AND SYMBOLS

- DG distributed generations
- UPS uninterruptible power supply
- VSC voltage source converters
- UPF unity power factor
- PWM pulse-width modulation
- HCC hysteresis current control
- PMSG permanent magnet synchronous generator
- PLL phase lock loop
- \( A, b, c \) phase order in \( a-b-c \) coordinate
- \( D, q, 0 \) phase order in \( d-q-0 \) coordinate
- \( V_{dc,ref ni} \) DC reference voltage of the \( i \)-th network converter
- \( I_{ni} \) output current of the \( i \)-th network converter
- \( P_{ni} \) output DC power of the \( i \)-th network converter
- \( R_{ni} \) equivalent resistance of the \( i \)-th network converter
- \( I_{M Ts} \) output current of the microturbine units
- \( I_{FCs} \) output current of the fuel cell units
- \( I_{L1} \) output current of the load converters No. 1
- \( I_{L2} \) output current of the load converters No. 2
- \( I_{L3} \) output current of the load converters No. 3
- \( I_{L4} \) current taken by load directly connected to DC bus
- \( I_c \) circulating current
- \( P_{MT,n} \) output power of \( n \)-th fuel cell and microturbine units
- \( P_{FC,n} \) output power of \( n \)-th fuel cell and microturbine units
- \( P_{net} \) total power consumed by all loads connected to the DC bus
- \( P_{L1} \) power consumed by \( L_1 \)
- \( P_{L2} \) power consumed by \( L_2 \)
- \( P_{L3} \) power consumed by \( L_3 \)
- \( P_{L4} \) power consumed by \( L_4 \)
- \( K \) controller gain
- \( \delta \) voltage droop in general
- \( \chi n \) reference active power of each network converter
- \( \chi n \) reference reactive power of each network converter
- \( i_{ref f i} \) reference current for each network converter for phase \( i \)
- \( P_{DG,ref i} \) reference active power for each DG unit
- \( P_{ref DG, i} \) reference current for each DG unit
- \( V_{ref f i} \) reference current for each load converter for phase \( i \)
- \( F \) frequency in general
- \( v_i \) instantaneous line-to-neutral voltage for phase \( i \)
- \( i_i \) instantaneous phase current for phase \( i \)

REFERENCES


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