

A MULTI-OBJECTIVE OPTIMIZATION FOR PERFORMANCE IMPROVEMENT OF THE Z-SOURCE ACTIVE POWER FILTER

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The high power dissipation is one of the most important problems of the z-source inverter (ZSI). By using an appropriate optimization scheme, the losses can be significantly reduced without any negative impact on the other characteristics of the inverter. In this paper, a multi-objective optimization is implemented in order to reduce the ZSI total losses as well as to improve the z-source active power filter (APF) performance. The optimization is focused on the four important objectives including power losses of the Z-source APF, the initial cost of the system components, the voltage and current ripples, and the boost factor of the z-source network. For these purposes, the multi-objective genetic algorithm (MOGA) is employed. The numerical and simulation results are presented to evaluate the optimization performance. The results show that a good balance can be achieved between the switching power losses, the voltage-current ripple levels, the component costs and the boost factor using the optimized parameters.

Keywords: active power filters, Z-source inverter, switching loss, parameter optimization, multi-objective genetic algorithms

1 INTRODUCTION

The active power filter is an effective device for mitigate the load current harmonics and compensate the reactive power. The inverter of the active power filter is one of the most important parts of it. The function of inverter is to generate the compensation current. In the traditional active filter topologies, a voltage source inverter (VSI) or current source inverter (CSI) are used [1–4]. These topologies have many disadvantages and limits, such as the need for a large capacitor in the DC-link, only buck mode operation, the requirement for dead time between PWM duty cycles, and noise issues due to electromagnetic interference [5]. To overcome these problems, a new inverter topology known as impedance source inverter (ZSI) has attracted a lot of attention recently [6–9]. Some advantages of ZSI compared to the previous structures are the ability to increase or decrease the voltage over a wide range by setting the shoot-through (ST) time interval, the possibility of shoot-through without damaging of the switches, a second order filtering by impedance network and power quality improvement, the high switching frequency of the impedance network which is 6 times more than inverter frequency leading to size reduction of the elements, less influence of EMI noise, and *etc* [10, 11]. Figure 1 shows the schematic of a three-phase ZSI active filter connected to the grid.

Despite its many benefits, one of the major problems in the ZSI topology is the high switching power loss versus traditional inverter structure [12–14].

In the previous literature, some techniques have been proposed to reduce the ZSI losses and improve the efficiency. In [14], the Si-based power devices of the ZSI are replaced by new SiC-based power devices. Although

the SiC-based power devices can partially reduce the total losses, the some disadvantages such as technological restrictions, limited availability, and need for high-temperature packaging techniques, that have not yet been developed, limit its widespread use [15]. In [16] and [17], reducing the switching losses is performed only by changing of the PWM pattern and ST time interval. Although appropriate adjustment of ST can effect on the inverter losses, but it is not enough. The loss compensation and the efficiency improvement in this method are not significant. In addition, this technique may have a negative effect on the boost factor (BF) of the ZSI.

It is possible to effectively reduce the overall losses of the ZSI by appropriate choice of the parameters and elements values. However, on the other hand, a large variation in the ZSI parameters can cause performance degradation, quality reduction of the waveforms, and cost rising. Therefore, finding the optimal points to establish a balance needs to solve optimization problem with multiple equations and parameters. Due to the nonlinear nature of the equations, the multi-objective optimization algorithm can achieve a good result. Thus, in this paper, an equilibrium is established between the switching power losses function, the initial cost of filter elements, the capacitor voltage and inductor current ripples, and the boost factor of the impedance network in the ZSI active power filter by multi-objective genetic algorithm (MOGA) to improve the filter performance.

The results evaluate effectiveness of optimized filter, where the loss reduction is equal to 39.5%, the cost reduction is 8.43%, and the current ripple improvement is 57.03%.

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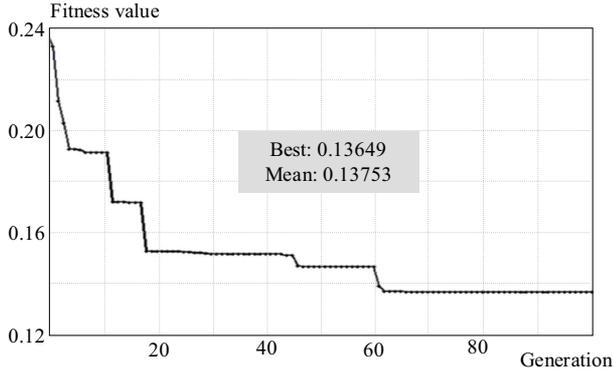


Fig. 2. MOGA search process for finding the optimal points in the response space

Table 1. System and parameters specifications

Source characteristic	$220v_{\text{rms}} - 50 \text{ Hz}$
Variations of L_1 and L_2	$[450 \ 2000] \ \mu\text{H}$
Variations of C_1 and C_2	$[300 \ 1500] \ \mu\text{F}$
Switching frequency (f_s)	10 KHz
Variations of T_0	$[0.0304 \ 0.0450] \ \text{ms}$
Input voltage V_{in}	270 V
Cut-off frequency	1 KHz
Output voltage $V_{(\text{inv}2, \text{L}2\text{L})}$	381 V_{rms}
$N_{(\text{con}/\text{disc})}$	1

Table 2. Weights of objective functions

W_1	0.45
W_2	0.25
W_3	0.10
W_4	0.20
α	0.8 (pu/ μH)
β	2 (pu/ μH)

Table 3. Tuned parameters for genetic algorithm

Chromosomes coding	Binary
Initial population	50
Generation of initial population	Random
Selection function	Roulette
Crossover type	Single point
Percentage of Crossover	%75
possibility of mutation	%5
Maximum generation	100

3 DEFINITION OF THE OBJECTIVE FUNCTIONS AND DECISION VARIABLES

In addition to the loss function, there are three other objectives that have to be considered for optimization the performance of ZSI active filter. Consequently, there will be a total of 4 optimization targets, as following:

- the power losses of the ZSI,
- the initial cost of the filter elements,
- the boost factor (BF) of the impedance network,
- the capacitor voltage and inductor current ripples.

The optimization algorithm is applied to the first and second objective functions to reduce losses and increase overall efficiency, and also reduce initial costs of the active filter structure. Hence, the parameters searching are carried out with the purpose of minimizing any two functions. But the target of third objective function is prevention of dropping of the boost factor and establishes the appropriate balance between the objectives. Thus the third objective function should be maximized. If the inductor and capacitor values of the impedance network choose less than of the certain level (for minimizing the cost function), the fluctuation of the capacitor voltage and inductor current waveforms increases. The ripple in the function is dependent to the parameters like capacitor and inductor value, and ST time which should be minimized. The conduction losses that are a major part of the total losses ($P_{C,ZSI}^{\text{IGBT}}$), diode conduction losses ($P_{C,ZSI}^{\text{D1}}$) and diode switching losses ($P_{S,ZSI}^{\text{D1}}$) are dependent on the selected parameters and it is possible to optimize its value. Therefore, the objective function of the ZSI losses is formed of the total conduction losses of the six numbers of IGBTs (in the 3-phase inverter) and total losses of the input diode.

$$F_1(T_0, L, C) = \left[\sum_{(n=1)}^6 P_{C,ZSI}^{\text{IGBT}_n} \right] + P_{C,ZSI}^{\text{D1}} + P_{S,ZSI}^{\text{D1}} \quad (11)$$

where T_0 is shoot-through time, L and C are inductor and capacitor of the impedance network, respectively. One important factor in the design of active filters is the initial and operation cost. There, the filter operation cost saving is obtained from the filter losses optimization, and to reduce initial cost, other objective function is defined encompassing the Z-network inductor and capacitor costs according to

$$F_2(L, C) = \text{Cost}(L, C) = \alpha \sum_{n=1,2} L_n + \beta \sum_{n=1,2} C_n \quad (12)$$

where α and β are cost rising coefficient for increasing in the amount of Z-source inverter inductance (mH) and capacitance (μF).

Among the advantages of Z-source inverter is the voltage boost capability which helps to remove extra DC/DC switching converter and large capacitor in DC-link. This capability can be achieved by adjusting the time period ST. Achievement of higher boost factor can be considered as one of the optimization objectives. Also, this ratio should not be less than specific threshold value (*ie* line voltage peak). For the boost factor, the Equation (13) is considered as objective function.

$$F_3(T_0) = \text{BF} = \left\{ \frac{1}{1 - 2(T_0/T)} \right\}. \quad (13)$$

As mentioned previously, if the Z-network inductor and capacitor values are selected less than certain level

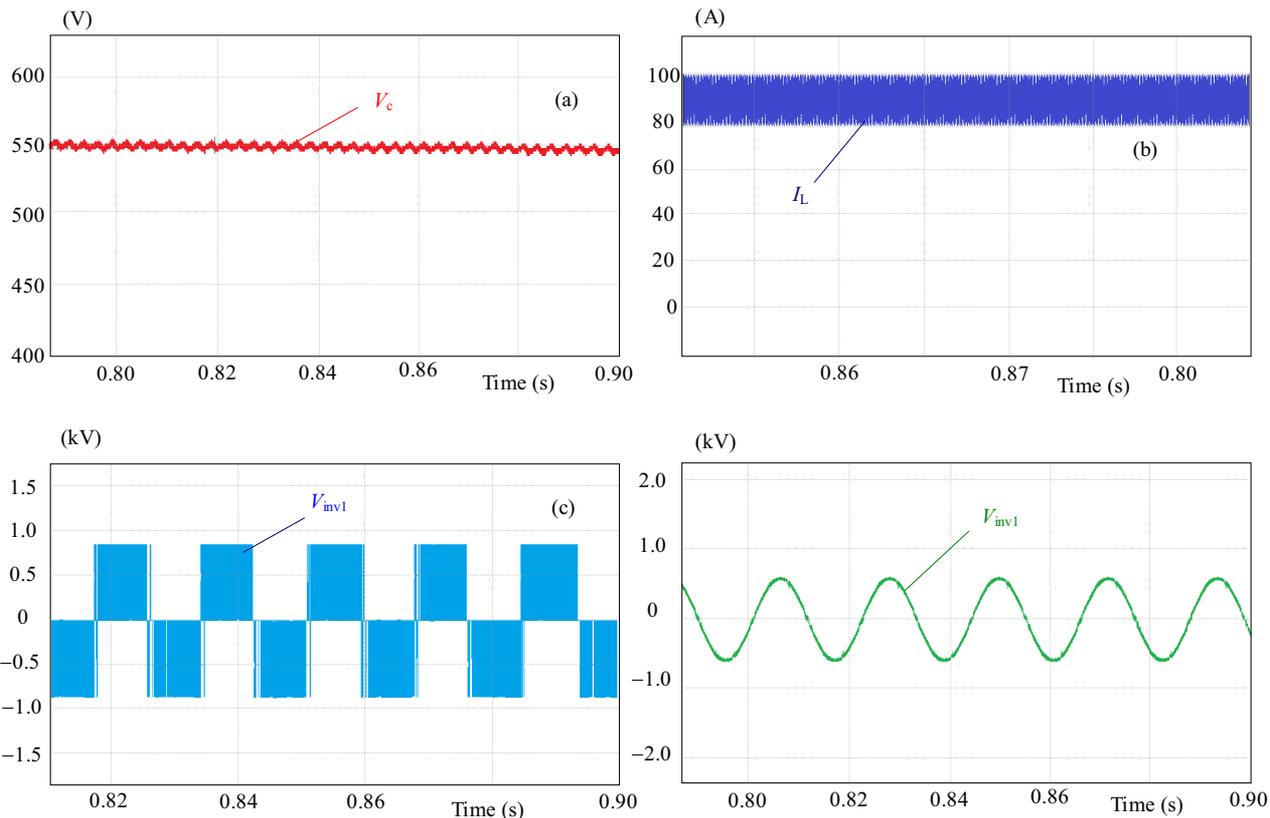


Fig. 3. Simulation waveforms: (a) — capacitor voltage, (b) — inductor current, (c) — ZSI output voltage before filtering, (d) — ZSI output voltage after filtering

Table 4. Comparison between non-optimal point and MOGA results

Characteristic	Non-optimal	MOGA
L	750 μH	1065.39 μH
C	860 μF	636.05 μF
T_0	0.0410 ms	0.0341 ms
P_{Tot}	2035.32 W	1229.47 W
Cost	4640.00 Unit	4248.82 Unit
$B.F$	5.550	3.125
ΔV_c	4.29 V	4.81 V
ΔI_L	48.34 A	17.77 A

(to reduce filter costs), the rate of fluctuation (ripple) in the capacitor voltage and the inductor current will increase and decrease the quality of the output voltage and current. Therefore, the inductor and capacitor values should be selected considering this issue, and then minimized fluctuations with parameters adjustment in the ripple relationship [18]. According to Equations (14) and (15), which are calculated for the ZSI structure elements, the ripple relations are a function of inductor and capacitor values, and shoot-through time interval.

$$\Delta V_c = \frac{I_L T_0}{L} \tag{14}$$

$$\Delta I_L = \frac{V_c T_0}{L} = \frac{T_0}{L} \frac{1 - (T_0/T)}{1 - 2(T_0/T)} V_{in} \tag{15}$$

where ΔV_c and ΔI_L are ripple of capacitor voltage and inductor current, respectively. Equation (15) is obtained

by relation between capacitor and input voltages in the ZSI structure by

$$V_c = \frac{1 - (T_0/T)}{1 - 2(T_0/T)} V_{in} . \tag{16}$$

The sum of two ripple equations in the ZSI is defined as fourth objective function which should be minimized. Hence, the objective function based on the normalized values of voltage and current ripples write as:

$$F_4(L, C, T_0) = \Delta V_c^{\text{norm}} + \Delta I_L^{\text{norm}} = \left[\frac{I_L T_0}{C} \right]' + \left[\frac{T_0}{L} \frac{1 - (T_0/T)}{1 - 2(T_0/T)} V_{in} \right]' \tag{17}$$

where ΔV_c^{norm} and ΔI_L^{norm} are normalized values of capacitor voltage and inductor current, respectively. With respect to the four mentioned objective functions, the process of this optimization is a multi-objective problem. There, in order to calculate the total objective function, the weighted-sum method has been employed [19]. Based on (18) to (19), in this method, all of the objective functions with certain weights are integrated together and the optimization is focused on the overall objective function [20].

$$F(x) = \{f_1(x), \dots, f_n(x)\} = w_1 f_1' + w_2 f_2' + \dots + w_n f_n' \tag{18}$$

$$\text{subject to: } g(x) \leq 0, \quad h(x) = 0. \tag{19}$$

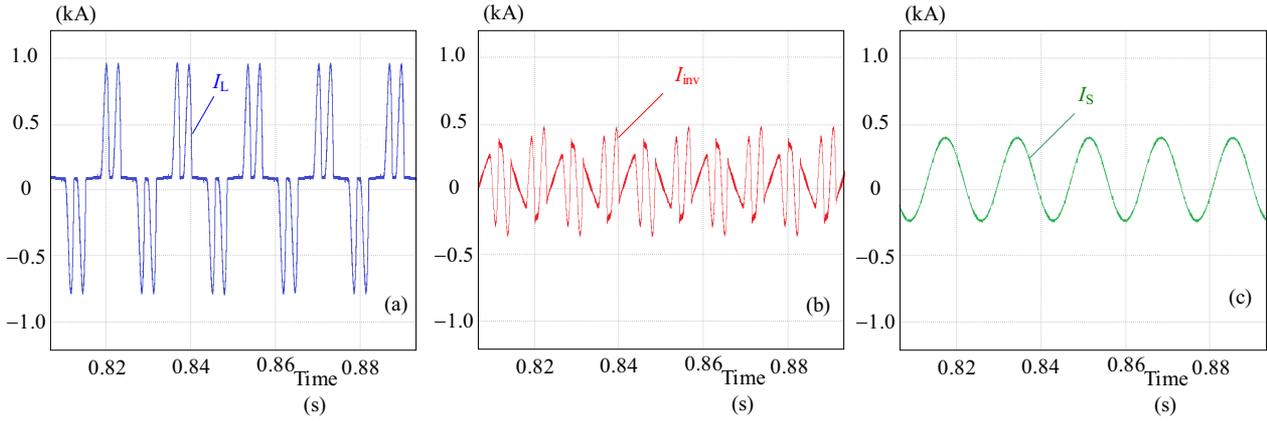


Fig. 4. (a) — Harmonic load current, (b) — inverter current, (c) — compensated source current

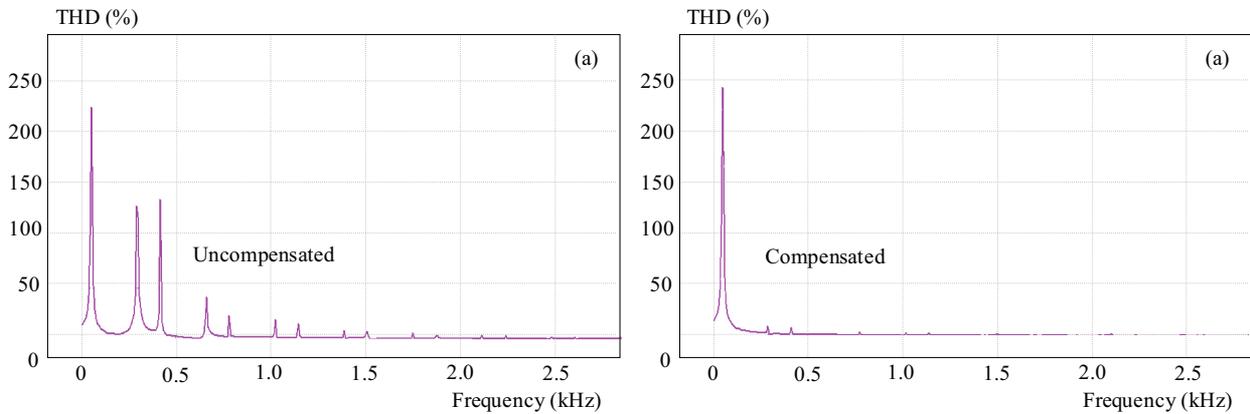


Fig. 5. Frequency spectrum of line current: (a) — load side, (b) — compensated source side

For the weights of functions

$$\sum_{i=1}^n w_i = 1. \quad (20)$$

should be fulfilled. Thus, the objective functions of this problem can be rewritten as an overall function according to

$$F'_T(T_0, L, C) = W_1 F'_1 + W_2 F'_2 + W_3 F'_{3,\text{modified}} + W_4 F'_4 \quad (21)$$

where W_1, W_2, W_3 and W_4 are weights of each of functions, respectively. F'_1, F'_2 and F'_4 are normalized objective functions, and $F'_{3,\text{modified}}$ is inverse normalized boost factor function. In fact, because the purpose is minimizing the overall objective function, the third objective function is corrected in equation

$$F_{3,\text{modified}}(T_0) = 1 - 2D_0 = 1 - 2\frac{T_0}{T}. \quad (22)$$

Because the objective functions have different scales, these functions need to be normalized. Therefore, each of

the objective functions are normalized using Equations (23) and (24), and are varied in the range $[0, 1]$.

$$F_i^* = \min(F_i), \quad i \in \{1, 2, \dots, n\}, \quad (23)$$

$$F'_i = \frac{F_i - F_i^*}{F_i^{\max} - F_i^*}, \quad i \in \{1, 2, \dots, n\}. \quad (24)$$

4 IMPLEMENTATION OF MULTI-OBJECTIVE GENETIC ALGORITHM (MOGA)

The overall objective function using the sum-weighted method is presented in equation

$$F'_T(T_0, L, C) = W_1 \left\{ \left[\sum_{n=1}^6 P_{C,ZSI}^{\text{IGBT}^n} \right] + P_{C,ZSI}^{\text{D1}} + P_{S,ZSI}^{\text{D1}} \right\}_{\text{norm}} + W_2 \left\{ \alpha \sum_{n=1,2} L_n + \beta \sum_{n=1,2} C_n \right\}_{\text{norm}} + W_3 \left\{ 1 - 2\frac{T_0}{T} \right\}_{\text{norm}} + W_4 \left\{ \frac{I_L T_0}{C} + \frac{T_0}{L} \frac{1 - (T_0/T)}{1 - 2(T_0/T)} V_{\text{in}} \right\}_{\text{norm}}. \quad (25)$$

To avoid extreme amounts of Z-network gain (boost factor) and voltage instability problem, and to preventing negative gain, the amount $\frac{T_0}{T}$ should be less than 5.0,

$$0 < \frac{T_0}{T} < 0.5. \quad (26)$$

5 OPTIMIZATION AND SIMULATION RESULTS

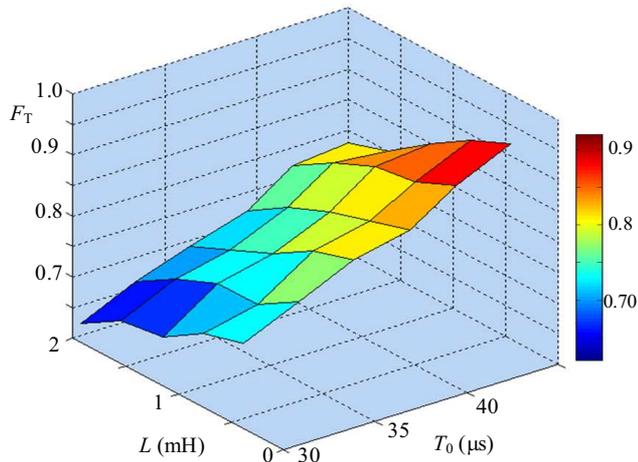


Fig. 6. The variations of overall objective function over Z-source inductance (L) and ST time (T_0)

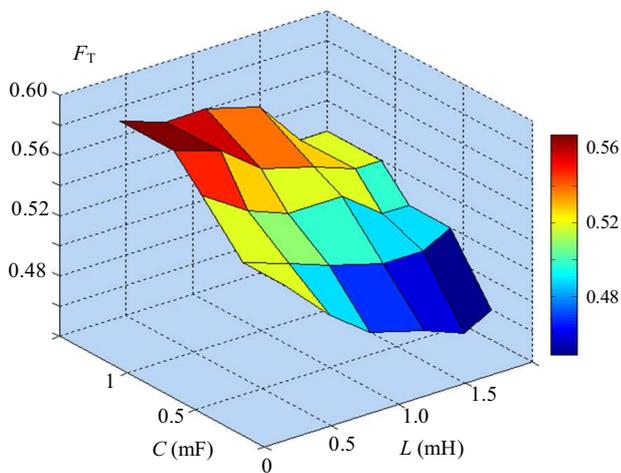


Fig. 7. Frequency spectrum of line current: (a) — load side, (b) — compensated source side

To calculate the lower limit of ST time (T_0), the minimum value of DC-link voltage should be calculated. This value is achieved with respect to the maximum output phase voltage.

$$\hat{v}_{ac} = M \frac{\hat{v}_{dc}}{2} \tag{27}$$

$$\Rightarrow \hat{v}_{dc} = \frac{2\hat{v}_{ac}}{M} \tag{28}$$

where \hat{v}_{ac} and \hat{v}_{dc} are the values of maximum output phase voltage and minimum DC-link voltage, respectively. The minimum limit of $\frac{T_0}{T}$ can be derived as

$$\left. \frac{T_0}{T} \right|_{\min} = \frac{1 - (\hat{v}_{dc}/v_{in})}{2} = \frac{1 - (2\hat{v}_{ac}/Mv_{in})}{2} \tag{29}$$

$$\Rightarrow 0.5 - \frac{\hat{v}_{ac}}{Mv_{in}} < \frac{T_0}{T} < 0.5. \tag{30}$$

Other constraints and parameters used for optimization the ZSI active filter have been provided in Tabs. 1 and 2.

The tuned parameters for the genetic algorithm search process in the problem space are presented in Tab. 3.

The genetic algorithm search process is implemented on the overall objective function using MATLAB software. Figure 2 shows the algorithm search for finding the optimal value of the fitness function.

The calculated parameters using genetic algorithm for minimizing the objective function of ZSI active filter, and the amount of switching losses, the cost function, the boost factor and the voltage and current ripples in both genetic algorithm method and non-optimal conditions (typical values that meet their constraints) are presented in Tab. 4.

Figure 3 shows the waveforms of the capacitor voltage (V_c), the inductor current (I_L), and the inverter output voltage before and after using low pass filter (V_{inv1}, V_{inv2}).

As can be seen from the results, after optimization with the MOGA, the value of losses function P_{ZSI}^{Tot} compared to non-optimal condition is reduced by 39.5%. Also, the inductor current ripple is decreased by 57.03%. However, a slight increase is observed in the voltage ripple equal to 10.81%, which is negligible considering the other benefits. The BF in the optimum condition is equal to 3.125 that is appropriate level. In addition, the value of cost function is reduced using by optimum parameters, which means a reduction in the initial cost of the active filter. Figure 4 shows the current waveforms of the ZSI active power filter.

By using the optimized ZSI active power filter, the level of (THD) in the load current is reduced from 78.39% to 5.44%, and the power factor is improved from 63.65% to 97.04%. A comparison between the frequency spectrums before and after compensation is presented in Fig. 5.

By implementing the multi-objective genetic algorithm optimization, the initial cost of ZSI active power filter is reduced by 8.43%. The variations of the overall objective function (F'_T) in terms of parameters changes are shown in Figs. 6 to 8.

6 CONCLUSIONS

This paper presented a multi-objective optimization on the Z-source active power filter to overcome the ZSI power loss problems and improvement of the active filter performance. The four important objective function including the power losses of the ZSI, The initial cost of the filter elements, the boost factor of the Z-network, the capacitor voltage and inductor current ripples was formed. The multi-objective genetic algorithm (MOGA)

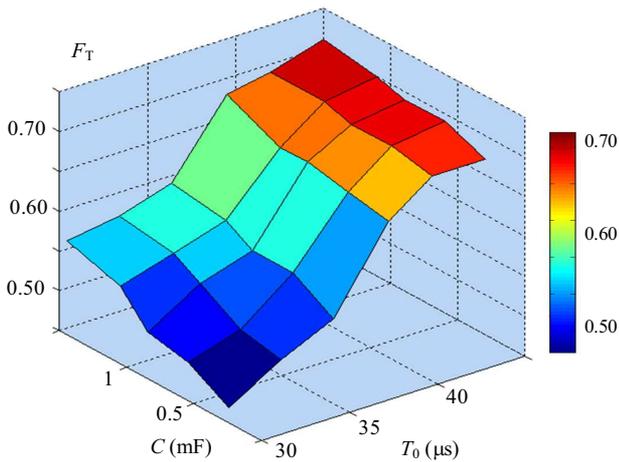


Fig. 8. The variations of overall objective function over Z-source capacitance (C) and ST time (T_0)

was applied to the overall objective function. The analysis of numerical and simulation results indicate a 39.5% reduction in the losses function, 57.03% improvement in the inductor current ripple, 8.43% reduction in the initial cost of impedance network as well as a good level of the boost factor by 3.125. Also, the operation of Z-source active filter is appropriate in the harmonic compensation of the non-linear load current.

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