This paper presents a pulse doubling technique in a 12-pulse ac-dc converter which supplies direct torque controlled motor drives (DTCIMDs) in order to have better power quality conditions at the point of common coupling. The proposed technique increases the number of rectification pulses without significant changes in the installations and yields in harmonic reduction in both ac and dc sides. The 12-pulse rectified output voltage is accomplished via two paralleled six-pulse ac-dc converters each of them consisting of three-phase diode bridge rectifiers. An autotransformer is designed to supply the rectifiers. The design procedure of magnets is in a way such that makes it suitable for retrofit applications where a six-pulse diode bridge rectifier is being utilized. Independent operation of paralleled diode-bridge rectifiers, i.e. dc-ripple re-injection methodology, requires a Zero Sequence Blocking Transformer (ZSBT). Finally, a tapped interphase reactor is connected at the output of ZSBT to double the pulse numbers of output voltage up to 24 pulses. The aforementioned structure improves power quality criteria at ac mains and makes them consistent with the IEEE-519 standard requirements for varying loads. Furthermore, near unity power factor is obtained for a wide range of DTCIMD operation. A comparison is made between 6-pulse, 12-pulse, and proposed converters from viewpoint of power quality indices. Results show that input current total harmonic distortion (THD) is less than 5% for the proposed topology at various loads.

**Keywords**: AC-DC converter, zigzag autotransformer, power quality, 24 pulse rectifier, direct torque controlled induction motor drive (DTCIMD)

1 INTRODUCTION

Recent advances in solid state conversion technology has led to the proliferation of variable frequency induction motor drives (VFIMDs) that are used in several applications such as air conditioning, blowers, fans, pumps for waste water treatment plants, textile mills, rolling mills etc [1]. The most practical technique in VFIMDs is direct torque controlled strategy in that it offers better performance rather than the other control techniques, direct torque controlled technique is implemented in voltage source inverter which is mostly fed from six-pulse diode bridge rectifier, Insulated Gate Bipolar Transistors (IGBTs) are employed as the VSI switches. The most important drawback of the six-pulse diode-bridge rectifier is its poor power factor injection of current harmonics into ac mains. The circulation of current harmonics into the source impedance yields in harmonic polluted voltages at the point of common coupling (PCC) and consequently resulting in undesired supply voltage conditions for customers in the vicinity. The value of current harmonic components which are injected into the grid by nonlinear loads such as DTCIMDs should be confined within the standard limitations. The most prominent standards in this field are IEEE standard 519 [2] and the International Electrotechnical Commission (IEC) 61000-3-2 [3].

According to considerable growth of Static Power Converters (SPCs) that are the major sources of harmonic distortion and as a result their power quality problems, researchers have focused their attention on harmonic eliminating solutions. Passive and active filters are compensating devices which are utilized in power grids to enhance power quality. However, they introduce some drawbacks. Passive filter installations are bulky and require extra area. Furthermore, they cause additional losses and the variations in resonance frequency influences their operation and consequently making their design complex. Likewise, active filters implementation is complicated and costly. Besides, their ratings should be analogous to load rating.

The aforementioned problems and harmonic pollution could be nearly resolved using multi-pulse AC-DC converters. Basically, Harmonic cancelation in multi-pulse converters is accomplished via two or more paralleled bridge rectifiers in which their supplying voltages are phase shifted according to the desired output voltage pulse number. Various schematics of 12-pulse AC-DC converters have been proposed by researchers so far [4-8]. Although, these topologies do not meet the IEEE standard requirements for permissible harmonic distortion. Obviously, more paralleled bridge rectifiers will result in higher pulse numbers and, consequently, better power quality conditions. On the contrary, the cost and complexity of the whole system will increase significantly. Reduced cost and complexity of AC-DC converters beside the improved power quality indices can be achieved by DC ripple re-injection method [9-16]. The zigzag-connected autotransformer-based 24-pulse topology [16]...
In this paper, a 24-pulse ac-dc converter is extracted from a 12-pulse ac-dc converter through adding a pulse doubling circuit in the DC link. The proposed design method will be suitable even when the transformer output voltages vary while keeping its 12-pulse operation. In the proposed structure, two three-leg diode-bridge rectifiers are paralleled via a Zero Sequence Blocking Transformer (ZSBT) and fed from an autotransformer. Hence, a 12-pulse output voltage is obtained. In order to double the number of pulses up to 24, a tapped Inter-Phase Reactor (IPR) with two additional diodes are included in the rectifiers output. This pulse multiplication works on the basis of ripple re-injection method, where the power of the circulating ripple frequency is fed back to the dc system via an IPR [9].

In other words, the removal of harmonics in 12-pulse converter is accomplished via the dc voltage ripple which is the frequency source for the derivation of adequate voltage and current waveforms. Ratings of IPR are small versus output apparent power. The number of turns in each IPR taps is such that the operation of diodes produces a near sinusoidal waveform in the ac line currents. Detailed design tips of the tapped IPR and totally the whole structure of 24-pulse ac-dc converter are described in this paper and the proposed converter is modeled and simulated in MATLAB to study its behavior and specifically to analyze the power quality indices at ac mains.

Furthermore, a 12-pulse ac-dc converter consisting of a zigzag autotransformer, two six-pulse diode bridge rectifiers paralleled through two IPTs, and with a DTCIMD load Fig. 1 is also designed and simulated to compare its operation with the proposed 24-pulse ac-dc converter. Simulation results of six-pulse, 12-pulse and proposed 24-pulse ac-dc converters feeding a DTCIMD load are scheduled and various quality criteria such as THD of ac mains current, power factor, displacement factor, distortion factor, and THD of the supply voltage at PCC are compared.
2 24-PULSE AC–DC CONVERTER

As mentioned previously, the pulse-doubling technique requires a zero-sequence-blocking transformer (ZSBT) and a diode-tapped inter-phase reactor to multiple the number of a pulses up to 24.

It is known that a 12-pulse rectified voltage can be made of two paralleled six-pulse three-phase (three-leg) diode-bridge rectifiers. The phase shift between two supplying voltages should be 30 degrees. Similarly, in order to implement a 12-pulse ac–dc converter through paralleling two bridge rectifiers, ie two 6-pulse rectifiers, two sets of three-phase voltages with a phase difference of 120 degrees between the voltages of each group and 30 degrees between the same voltages of the two groups are required. Accordingly, each bridge rectifier consists of three common-anode and three common-cathode diodes (two three-leg rectifiers). A zigzag autotransformer is designed to produce the three phase voltages which are shown in Fig. 2. An overall schematic of the proposed 24-pulse ac–dc converter is shown in Fig. 3.

2.1 Design of Autotransformer for Retrofit Applications

The aforementioned two voltage sets are called as \((V_a, V_o, V_{o3})\) and \((V_{o1}, V_{o2}, V_{o3})\) that are fed to rectifiers I and II, respectively. The same voltages of the two groups, ie \(V_{o1}\) and \(V_{o4}\), are phase displaced of 30 degrees. \(V_a\) and \(V_{o1}\) has a phase shift of +15 and −15 degrees from the input voltage of phase A, respectively. According to phasor diagram, the three-phase voltages are made from ac main phase and line voltages with fractions of the primary winding turns which are expressed with the following relationships. Consider three-phase voltages of primary windings represented by their phasors \((V)\)

\[
V_A = V_o \angle 0\degree, \\
V_B = V_o \angle -120\degree, \\
V_c = V_o \angle 120\degree, \\
\]

where, three-phase voltages are

\[
V_{o1} = V_S \angle 15\degree, \\
V_{o3} = V_S \angle -105\degree, \\
V_{o1} = V_S \angle 135\degree. \\
\]

Input voltages for converter 1 are

\[
V_{a1} = K_1(V_AB - V_CA) - K_2V_BC, \\
V_{b1} = K_1(V_BC - V_AB) - K_2V_CA, \\
V_{c1} = K_1(V_CA - V_BC) - K_2V_AB. \\
\]

Input voltages for converter 2 are

\[
V_{a2} = K_1(V_AB - V_CA) + K_2V_BC, \\
V_{b2} = K_1(V_BC - V_AB) + K_2V_CA, \\
V_{c2} = K_1(V_CA - V_BC) + K_2V_AB. \\
\]

Constants \(K_1 - K_2\) are calculated using (2)–(6) to obtain the required windings turn numbers to have the desired phase shift for the two voltage sets

\[
K_1 = 0.3219, \quad K_2 = 0.1494. \\
\]
The value of output voltage in multi-pulse rectifiers boosts relative to the output voltage of a six-pulse converter making the multi-pulse rectifier inappropriate for retrofit applications. For instance, with the autotransformer arrangement of the proposed 24-pulse converter, the rectified output voltage is 4% higher than that of six-pulse rectifier. This will be accomplished via modifications in the tapping positions on the windings as shown in Fig. 4. It should be noted that with this approach, the desired phase shift is still unchanged. In a manner similar to section 2.1, the following equations can be derived

\[ |V_S| = V_S = 0.96|V_A| = 0.96V_A. \]  

Accordingly, the values of constants \( K_1 \) and \( K_2 \) are changed for retrofit applications as

\[ K_1 = 0.3090, \quad K_2 = 0.1434. \]  

The values of \( K_1 \) and \( K_2 \) establish the essential turn numbers of the autotransformer windings to have the required output voltages and phase shifts.

The kilovolt-ampere rating of the autotransformer is calculated as [4]

\[ P = \frac{1}{2} \sum V_{\text{winding}}I_{\text{winding}} \text{ (kVA)} \]  

where \( V_{\text{winding}} \) is the voltage across each autotransformer winding and \( I_{\text{winding}} \) indicates the full load current of the winding. Apparent power ratings of the tapped-interphase reactor and zero-sequence-blocking transformer (ZSBT) are also calculated in a same way.

2.3 Interphase Transformer

The theory of pulse multiplication has been presented in [9] where a tapped inter-phase reactor along with two additional diodes are used to double the number of pulses in the supply line current resulting in current harmonic reduction. Afterwards, tapped interphase reactor was used in [17–22] to double the number of pulses in 12-pulse ac-dc converters. Furthermore, this type of multiplier was also served in paralleled thyristor bridge rectifiers [23]. Likewise, we used a tapped interphase reactor (IPR) to extract a 24-pulse current from two paralleled 6-pulse rectifiers.

The IPR and tapped diodes are shown in Fig. 5. For the pulse multiplication process, it is necessary to ensure that the average output voltages of bridges are equal and phase shifted of 30 degrees. As two 6-pulse rectifiers are paralleled, the voltage across the interphase transformer, \( V_m \), has a frequency 6 times that of the supply system. Therefore, size, weight and volume of the transformer reduce relative to rectifiers with a less pulse number. \( V_m \) is an alternating voltage with both positive and negative half cycles. Hence, \( D_1 \) conducts when the \( V_m \) is positive and, on the other hand, \( D_2 \) conducts when \( V_m \) is negative. The MMF equivalence between the windings when \( D_1 \) is on yields

\[ i_{dc1}N_A = i_{dc2}N_B \]  

where \( N_A \) and \( N_B \) are number of turns as shown for IPR. We also have

\[ i_{dc1} + i_{dc2} = i_{dc}. \]  

Using (13) and (14), output current of the two rectifiers are calculated as follows

\[ i_{dc1} = (0.5 + K_t)i_{dc}, \quad i_{dc2} = (0.5 - K_t)i_{dc}. \]  

In the above equation, \( N_0 = N_A + N_B \) and \( K_t = (N_B - 0.5N_0)/N_0 \). The same relations can be written when \( V_m \) is in its negative half cycle. Therefore, according to MMF equation, the magnitude of output currents changes which results in pulse multiplication in the supply current. In [11], it is proved that \( K_t \) should be equal to 0.2457 to eliminate the harmonic currents up to the 21st order which can be applied in this application too.
Table 1. Comparison of simulated power quality parameters of the DTCIMD fed from different ac-dc converters

<table>
<thead>
<tr>
<th>Sr. No.</th>
<th>Topology of $V_{ac}$</th>
<th>AC Mains % THD of $I_{SA}$ (A) at Light Load</th>
<th>% THD of $I_{SA}$ (A) at Full Load</th>
<th>Distortion Factor, DF</th>
<th>Displacement Factor, DPF</th>
<th>Power Factor, PF</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>6-pulse</td>
<td>5.63</td>
<td>10.25</td>
<td>52.56</td>
<td>52.80</td>
<td>28.52</td>
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<td>0.959</td>
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<td></td>
<td>0.872</td>
<td>0.948</td>
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<tr>
<td>2</td>
<td>12-pulse</td>
<td>3.66</td>
<td>10.47</td>
<td>53.58</td>
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<td></td>
<td>0.983</td>
<td>0.977</td>
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<tr>
<td>3</td>
<td>24-pulse</td>
<td>3.12</td>
<td>10.50</td>
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<td>5.77</td>
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<td>0.994</td>
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</table>

2.4 Zero Sequence Blocking Transformer

In parallel-rectifier configurations, the two converters cannot be directly paralleled. Because, the output voltages are phase-shifted thereby unwanted conduction sequence of diodes is probable. Therefore, a zero-sequence blocking transformer is required to ensure the independent operation of two paralleled rectifiers. In the proposed 24-pulse converter, the voltage frequency of ZSBT is three times that of the supply system and it shows high impedance zero sequence (and its multiples) current harmonics and prevents them to flow. Furthermore, high ripple frequency of the supply voltage in ZSBT makes it small and light.

3 MATLAB-BASED SIMULATION

The designed configurations were simulated using Matlab/Simulink software and power system block set (PSB) toolbox. In this model, a three-phase 460 V and 60 Hz network is utilized as the supply for the 24-pulse converter. The designed autotransformer is modeled via three multi-winding transformers. Multi-winding transformer block is also used to model ZSBT and IPT.

At the converter output, a series inductance ($L$) and a parallel capacitor ($C$) as the dc link are connected to IGBT-based Voltage Source Inverter (VSI). VSI drives a squirrel cage induction motor employing direct torque controlled strategy. The simulated motor is 50 hp (37.3 kW), 4-pole, and Y-connected. Detailed data of motor are listed in Appendix A. Simulation results are
Fig. 10. Input current waveform of ac-dc converters and its harmonic spectrum at light load and full load at: (a), (b) – 6-pulse, (c), (d) – 12-pulse, and (e), (f) – 24-pulse depicted in Figs. 6–12. Power quality parameters are also listed in Table 1 for 6-pulse, 12-pulse, and 24-pulse ac-dc converters.

4 RESULTS AND DISCUSSION

Table 1 lists the power quality indices obtained from the simulation results of the 6-pulse, 12-pulse, and 24-pulse converters. Matlab block diagram of 24-pulse ac-dc converter system simulation, as shown in Fig. 8. Figure 6 depicts two groups of three-phase voltage waveforms with a phase shift of 30 degrees between the same voltages of each group. The voltage across the interphase transformer (shown in Fig. 7) has the frequency equal to 6 times that of the supply which results in a significant reduction in volume and cost of magnetics.

The current waveforms of pulse doubling diodes are shown in Fig. 8. Diode D1 conducts when the voltage across the IPT is positive and, conversely, D2 is on when the voltage across the IPT is in its negative half-cycle. The magneto motive force (MMF) equivalence of the IPT windings are formulated in equation (13) when D1 is on. This conduction sequence of the diodes is the basis of the pulse doubling technique. The 24-pulse converter output voltage (shown in Fig. 9) is almost smooth and free of ripples and its average value is 606.4 volts which is approximately equal to the DC link voltage of a six-pulse rectifier (607.9 volts). This makes the 24-pulse converter suitable for retrofit applications.

Input current waveforms and its harmonic spectrum of the 6-pulse, 12-pulse, and 24-pulse converters extracted and shown in Fig. 10 (a, b), respectively to check their
consistency with the limitations of the IEEE standard 519. These harmonic spectra are obtained when induction motor operates under light load (20% of full load) and full load conditions. Hence, input current THD of this converter will be relatively a large amount and is equal to 28.52% and 52.80% for full load and light load conditions that are not within the standard margins.

The THD of ac mains current of 12-pulse ac-dc converter at full load is 7.36%, which deteriorates to 13.19% at light load (shown in Fig. 10 (c, d)), which is also not within IEEE Standard 519 limits. On the other hand, as shown in Fig. 10 (e, f), 24-pulse converter has an acceptable current THD (5.77% for light load and 4.51% for full load conditions). In this configuration, low order harmonics up to 21st are eliminated in the supply current.

In general, the largely improved performance of the 24-pulse converter makes the power quality indices such as THD of supply current and voltage (THDi and THDv), displacement power factor (DPF), distortion factor (DF), and power factor (PF) satisfactory for different loading conditions. The aforementioned criteria are listed in Table 1 for the three types of converters.

Input current THD and power factor variations are also shown in Figs. 11 and 12 respectively, for 6-pulse and 24-pulse ac-dc converters. Results show that the input current corresponding to the proposed configuration has an almost unity power factor. Furthermore, in the worst case (light loads) the current THD has reached below 5% for the proposed topology.

Different power quality indices of the proposed topology under different loading conditions are shown in Table 2. Results show that even under load variations, the 24-pulse converter has an improved performance and the current THD is always less than 5% for all loading conditions.

### 5 CONCLUSION

In this paper a zigzag-connected autotransformer was designed and modeled to make a 24-pulse ac-dc converter with DTCIMD load. Afterwards, the proposed design procedure was modified for retrofit applications. A zero-sequence-blocking transformer was added to ensure the independent operation of paralleled rectifiers and a tapped inter-phase reactor was used to double the number of pulses in the ac mains currents. The increased number of pulses results in the frequency increase of the supply voltages of ZSBT and IPR, thereby, decreasing the size and volume of the transformers. Simulation results prove that, for the proposed topology, input current distortion factor is in a good agreement with IEEE 519 requirements. Current THD is less than 5% for varying loads. It was also observed that the input power factor is close
to unity resulting in reduced input current for DTCIMD load.

**Appendix**

**Motor and Controller Specifications**

Three-phase squirrel cage induction motor — 50 hp (37.3 kW), three phase, four pole, Y-connected, 460 V, 60 Hz. \( R_s = 0.0148 \Omega; \) \( R_f = 0.0092 \Omega; \) \( X_{ls} = 1.14 \Omega; \) \( X_{lf} = 1.14 \Omega; \) \( X_{Lm} = 3.94 \Omega; \) \( J = 3.1 \text{Kg m}^2.\) Controller parameters: PI controller \( K_P = 300; \) \( K_I = 2000.\) DC link parameters: \( L_d = 2 \text{mH}; \) \( C_d = 3200 \mu F.\) Source impedance: \( Z_s = j0.1884 \Omega (= 3\%).\)

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